

**SESSION : 2025-26**

**DPP**  
DAILY PRACTICE PROBLEMS

**CLASS : XII<sup>th</sup>**

**SUBJECT : MATHS**

**DATE :**

**DPP NO. :1**

**Topic :-INVERSE TRIGONOMETRIC FUNCTIONS**

1.  $\left(\frac{3}{5}\right) + \left(\frac{1}{7}\right) =$   
a)  $\frac{\pi}{4}$                       b)  $\frac{\pi}{2}$                       c)  $\left(\frac{4}{5}\right)$                       d)  $\pi$
2. If  $xy + yz + zx = 1$ , then  $x + y + z =$   
a)  $\pi$                       b)  $\pi/2$                       c) 1                      d) none of these
3. If  $x^2 + y^2 + z^2 = r^2$ , then  $\left(\frac{xy}{zr}\right) + \left(\frac{yz}{xr}\right) + \left(\frac{xz}{yr}\right)$  is equal to  
a)  $\pi$                       b)  $\frac{\pi}{2}$                       c) 0                      d) None of these
4. If  $f(x) = \left\{\frac{\sqrt{3}}{2}x - \frac{1}{2}\sqrt{1-x^2}\right\}$ ,  $-\frac{1}{2} \leq x \leq 1$ , then  $f(x)$  is equal to  
a)  $\frac{1}{2} - x$                       b)  $x - \frac{\pi}{6}$                       c)  $x + \frac{\pi}{6}$                       d) None of these
5.  $\left(\frac{1}{2}\right) + 2\left(\frac{1}{2}\right)$  is equal to  
a)  $\frac{\pi}{6}$                       b)  $\frac{\pi}{3}$                       c)  $\frac{2\pi}{3}$                       d)  $\frac{\pi}{4}$
6. The solution of  $2\theta + 3\theta = \frac{\pi}{4}$  is  
a)  $\frac{1}{\sqrt{3}}$                       b)  $\frac{1}{3}$                       c)  $\frac{1}{6}$                       d)  $\frac{1}{\sqrt{6}}$
7. The value of  $\left(-\frac{1}{2}\right)$  among the following, is  
a)  $\frac{9\pi}{3}$                       b)  $\frac{8\pi}{3}$                       c)  $\frac{5\pi}{3}$                       d)  $\frac{11\pi}{3}$
8. If  $\tan \tan \theta + \tan \tan \left(\frac{\pi}{3} + \theta\right) + \tan \tan \left(-\frac{\pi}{3} + \theta\right) = a \tan \tan 3\theta$ , then  $a$  is equal to  
a)  $\frac{1}{3}$                       b) 1                      c) 3                      d) None of these
9. The value of  $\frac{3}{4} + \frac{5}{13}$  is  
a)  $\frac{63}{65}$                       b)  $\frac{12}{13}$                       c)  $\frac{65}{68}$                       d)  $\frac{5}{12}$

10. The value of  $x$  for which  $(\cos \cos 4) > 3x^2 - 4x$  is
- a)  $\left(0, \frac{2+\sqrt{6\pi-8}}{3}\right)$  b)  $\left(\frac{2-\sqrt{6\pi-8}}{3}, 0\right)$   
c)  $(-2, 2)$  d)  $\left(\frac{2-\sqrt{6\pi-8}}{3}, \frac{2+\sqrt{6\pi-8}}{3}\right)$
11. If  $x \in (-\infty, 1)$ , then  $\left(\frac{2x}{1-x^2}\right)$  equals
- a)  $2x$  b)  $-\pi + 2x$  c)  $\pi + 2x$  d) None of these
12. If  $\frac{1}{\sqrt{2}} \leq x \leq 1$ , then  $(2x\sqrt{1-x^2})$  equals
- a)  $2x$  b)  $\pi - 2x$  c)  $-\pi - 2x$  d) None of these
13.  $\frac{\alpha^3}{2} \operatorname{cosec}^2\left(\frac{1}{2} \frac{\alpha}{\beta}\right) + \frac{\beta^3}{2} \left(\frac{1}{2} \left(\frac{\beta}{\alpha}\right)\right)$  is
- a)  $(\alpha - \beta)(\alpha^2 + \beta^2)$  b)  $(\alpha + \beta)(\alpha^2 - \beta^2)$   
c)  $(\alpha + \beta)(\alpha^2 + \beta^2)$  d) None of these
14. If  $\sum_{i=1}^{20} x_i = 10\pi$ , then  $\sum_{i=1}^{20} x_i$  is equal to
- a) 20 b) 10 c) 0 d) None of these
15. Which one of the following is correct?
- a)  $\tan \tan 1 > 1$  b)  $\tan \tan 1 < 1$  c)  $\tan \tan 1 = 1$  d) None of these
16. If  $\alpha = \frac{\sqrt{3}}{2} + \frac{1}{3}$  and  $\beta = \frac{\sqrt{3}}{2} + \frac{1}{3}$ , then
- a)  $\alpha > \beta$  b)  $\alpha = \beta$  c)  $\alpha < \beta$  d)  $\alpha + \beta = 2\pi$
17.  $2\left(\frac{1}{3}\right) + \left(\frac{1}{7}\right)$  is equal to
- a)  $\left(\frac{49}{29}\right)$  b)  $\frac{\pi}{2}$  c)  $-\left(\frac{49}{29}\right)$  d)  $\frac{\pi}{4}$
18.  $\tan \tan \left[\frac{1}{2}\left(\frac{2a}{1+a^2}\right) + \frac{1}{2}\left(\frac{1-a^2}{1+a^2}\right)\right]$  is equal to
- a)  $\frac{2a}{1+a^2}$  b)  $\frac{1-a^2}{1+a^2}$  c)  $\frac{2a}{1-a^2}$  d) None of these
19. The sum of the infinite series  $2 + 8 + 18 + 32 + \dots$  is
- a)  $\pi$  b)  $\frac{\pi}{2}$  c)  $\frac{\pi}{4}$  d) None of these
20. If  $\left(\frac{a}{x}\right) + \left(\frac{b}{x}\right) = \frac{\pi}{2}$ , then  $x$  is equal to
- a)  $\sqrt{ab}$  b)  $\sqrt{2ab}$  c)  $2ab$  d)  $ab$

**SESSION : 2025-26**

**CLASS : XII<sup>th</sup>**

**DATE :**

**SUBJECT : MATHS**

**DPP NO. :2**

## Topic :-INVERSE TRIGONOMETRIC FUNCTIONS

1. If  $x_1, x_2, x_3, x_4$  are the roots of the equation  $x^4 - x^3 \sin \sin 2\beta - x \cos \cos \beta - \sin \sin \beta = 0$ , then  $+x_2 + x_3 + x_4$  is equal to  
 a)  $\beta$                                       b)  $\frac{\pi}{2} - \beta$                                       c)  $\pi - \beta$                                       d)  $-\beta$
2. If  $x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ , then the value of  $\left(\frac{\tan \tan x}{4}\right) + \left(\frac{3 \sin \sin 2x}{5+3 \cos \cos 2x}\right)$  is  
 a)  $\frac{x}{2}$                                       b)  $2x$                                       c)  $3x$                                       d)  $x$
3.  $\frac{\alpha^3}{2} \operatorname{cosec}^2 \left(\frac{1}{2} \frac{\alpha}{\beta}\right) + \frac{\beta^3}{2} \left(\frac{1}{2} \left(\frac{\beta}{\alpha}\right)\right)$  is  
 a)  $(\alpha - \beta)(\alpha^2 + \beta^2)$                       b)  $(\alpha + \beta)(\alpha^2 - \beta^2)$                       c)  $(\alpha + \beta)(\alpha^2 + \beta^2)$                       d) None of these
4. If  $-1 \leq x \leq 0$ , then  $(2x^2 - 1)$  equals  
 a)  $2x$                                       b)  $\pi - 2x$                                       c)  $2\pi - 2x$                                       d)  $-2x$
5. If  $\frac{3}{5} - \frac{4}{5} = x$ , then  $x$  is equal to  
 a) 0                                      b) 1                                      c) -1                                      d) None of these
6. If  $x = \operatorname{cosec}^{-1} y$ , then  $\frac{1}{x} + \frac{1}{y} =$   
 a)  $\pi$                                       b)  $\frac{\pi}{4}$                                       c)  $-\frac{\pi}{2}$                                       d)  $\frac{\pi}{2}$
7.  $(2) + \operatorname{cosec}^2 (3)$  is equal to  
 a) 1                                      b) 5                                      c) 10                                      d) 15
8. If  $-1 \leq x \leq -\frac{1}{2}$  then  $(3x - 4x^3)$  equals  
 a)  $3x$                                       b)  $\pi - 3x$                                       c)  $-\pi - 3x$                                       d) None of these
9.  $\tan \tan \frac{2\pi}{5} - \tan \tan \frac{\pi}{15} - \sqrt{3} \tan \tan \frac{2\pi}{5} \tan \tan \frac{\pi}{15}$  is equal to  
 a)  $-\sqrt{3}$                                       b)  $\frac{1}{\sqrt{3}}$                                       c) 1                                      d)  $\sqrt{3}$

10. The value of  $\tan \tan \left\{ \left( -\frac{2}{7} \right) - \frac{\pi}{2} \right\}$  is  
 a)  $\frac{2}{3\sqrt{5}}$                       b)  $\frac{2}{3}$                       c)  $\frac{1}{\sqrt{5}}$                       d)  $\frac{4}{\sqrt{5}}$
11. The value of  $\sin \sin \left( \frac{1}{3} + 3 \right) + \cos \cos \left( \frac{1}{2} + 2 \right)$  is  
 a) 1                      b) 2                      c) 3                      d) 4
12. If  $-\frac{1}{\sqrt{3}} < x < \frac{1}{\sqrt{3}}$ , then  $\left( \frac{3x-x^3}{1-3x^2} \right)$  equals  
 a)  $3x$                       b)  $-\pi + 3x$                       c)  $\pi + 3x$                       d) None of these
13.  $\sin \sin \left( \frac{14}{25} \right) =$   
 a)  $-\frac{1}{\sqrt{10}}$                       b)  $\frac{1}{\sqrt{10}}$                       c)  $-\frac{1}{10}$                       d)  $\frac{1}{10}$
14. The solution of  $2x + 3x = \frac{\pi}{4}$  is  
 a)  $\frac{1}{6}$                       b)  $-1$                       c)  $\left( \frac{1}{6}, -1 \right)$                       d) None of these
15.  $\frac{4}{5} + 2\frac{1}{3}$  is equal to  
 a)  $\frac{\pi}{3}$                       b)  $\frac{\pi}{4}$                       c)  $\frac{\pi}{2}$                       d) 0
16. The equation  $2x + x = \frac{11\pi}{6}$  has  
 a) No solution                      b) Only one solution                      c) Two solutions                      d) Three solutions
17. The value of  $\left( \cos \cos \frac{5\pi}{3} \right) + \left( \cos \cos \frac{5\pi}{3} \right)$  is  
 a)  $\frac{10\pi}{3}$                       b) 0                      c)  $\frac{\pi}{2}$                       d)  $\frac{5\pi}{3}$
18. The value of  $\left( \frac{\sqrt{3}}{2} \right) - \left( \frac{1}{2} \right)$  is  
 a)  $45^\circ$                       b)  $90^\circ$                       c)  $15^\circ$                       d)  $30^\circ$
19. If  $x + (1 - x) = x$ , then  $x$  equals  
 a) 1, -1                      b) 1, 0                      c)  $0, \frac{1}{2}$                       d) None of these
20.  $\tan \tan \left( \frac{\pi}{4} + \frac{1}{2}x \right) + \tan \tan \left( \frac{\pi}{4} - \frac{1}{2}x \right), x \neq 0$  is equal to  
 a)  $x$                       b)  $2x$                       c)  $\frac{2}{x}$                       d) None of these

## Topic :-INVERSE TRIGONOMETRIC FUNCTIONS

1.  $5 \cos^{-1} \left( \frac{1-x^2}{1+x^2} \right) + 7 \sin^{-1} \left( \frac{2x}{1+x^2} \right) - 4 \tan^{-1} \left( \frac{2x}{1-x^2} \right) - \tan^{-1} x = 5\pi$ , then  $x$  is equal to  
 a) 3                                      b)  $-\sqrt{3}$                                       c)  $\sqrt{2}$                                       d)  $\sqrt{3}$
2. If  $\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \frac{3\pi}{2}$  and  $f(1) = 2$ ,  
 $f(p+q) = f(p) \cdot f(q), \forall p, q \in R$ , then  
 $x^{f(1)} + y^{f(2)} + z^{f(3)} - \frac{(x+y+z)}{x^{f(1)}+y^{f(2)}+z^{f(3)}}$  is equal to  
 a) 0                                      b) 1                                      c) 2                                      d) 3
3.  $\cot^{-1}(\sqrt{\cos \alpha}) - \tan^{-1}(\sqrt{\cos \alpha}) = x$ , then  $\sin x$  is equal to  
 a)  $\tan^{-2} \left( \frac{\alpha}{2} \right)$                                       b)  $\cot^2 \left( \frac{\alpha}{2} \right)$                                       c)  $\tan \alpha$                                       d)  $\cot \left( \frac{\alpha}{2} \right)$
4. The value of  $\cot^{-1} 9 + \operatorname{cosec}^{-1} \frac{\sqrt{41}}{4}$  is  
 a)  $\frac{\pi}{2}$                                       b)  $\frac{\pi}{4}$                                       c)  $\frac{\pi}{3}$                                       d)  $\pi$
5.  $\sum_{m=1}^n \tan^{-1} \left( \frac{2m}{m^4+m^2+2} \right)$  is equal to  
 a)  $\tan^{-1} \left( \frac{n^2+n}{n^2+n+2} \right)$                                       b)  $\tan^{-1} \left( \frac{n^2-n}{n^2-n+2} \right)$                                       c)  $\tan^{-1} \left( \frac{n^2+n+2}{n^2+n} \right)$                                       d) None of these
6. If  $\cos^{-1} \frac{3}{5} - \sin^{-1} \frac{4}{5} = \cos^{-1} x$ , then  $x$  is equal to  
 a) 0                                      b) 1                                      c) -1                                      d) None of these
7. If  $\cot(\cos^{-1} x) = \sec \left( \tan^{-1} \frac{a}{\sqrt{b^2-a^2}} \right)$ , then  $x$  is equal to  
 a)  $\frac{b}{\sqrt{2b^2-a^2}}$                                       b)  $\frac{a}{\sqrt{2b^2-a^2}}$                                       c)  $\frac{\sqrt{2b^2-a^2}}{a}$                                       d)  $\frac{\sqrt{2b^2-a^2}}{b}$
8. The equation  $\sin^{-1} x - \cos^{-1} x = \cos^{-1} \left( \frac{\sqrt{3}}{2} \right)$  has  
 a) No solution                                      b) Unique solution  
 c) Infinite number of solutions                                      d) None of the above
9. If  $\theta = \sin^{-1} x + \cos^{-1} x - \tan^{-1} x \geq 0$ , then the smallest interval in which  $\theta$  lies, is given by

a)  $\frac{\pi}{2} \leq \theta \leq \frac{3\pi}{4}$

b)  $-\frac{\pi}{4} \leq \theta \leq 0$

c)  $0 \leq \theta \leq \frac{\pi}{4}$

d)  $\frac{\pi}{4} \leq \theta \leq \frac{\pi}{2}$

10. Solution of the equation  $\cot^{-1} x + \sin^{-1} \frac{1}{\sqrt{5}} = \frac{\pi}{4}$  is

a)  $x = 3$

b)  $x = \frac{1}{\sqrt{5}}$

c)  $x = 0$

d) None of these

11.  $\sin\left(\frac{1}{2}\cos^{-1}\frac{4}{5}\right)$  is equal to

a)  $-\frac{1}{\sqrt{10}}$

b)  $\frac{1}{\sqrt{10}}$

c)  $-\frac{1}{10}$

d)  $\frac{1}{10}$

12. If  $\sin^{-1}\left(\frac{3}{x}\right) + \sin^{-1}\left(\frac{4}{x}\right) = \frac{\pi}{2}$ , then  $x$  is equal to

a) 3

b) 5

c) 7

d) 11

13. If  $[\cot^{-1} x] + [\cos^{-1} x] = 0$ , where  $x$  is a non-negative real number and  $[.]$  denotes the greatest integer function, then complete set of values of  $x$  is

a)  $(\cos 1, 1]$

b)  $(\cot 1, 1)$

c)  $(\cos 1, \cot 1)$

d) None of these

14. If  $3 \sin^{-1} \frac{2x}{1+x^2} - 4 \cos^{-1} \frac{1+x}{1+x^2} + 2 \tan^{-1} \frac{2x}{1-x^2} = \frac{\pi}{3}$ , then value of  $x$  is

a)  $\sqrt{3}$

b)  $\frac{1}{\sqrt{3}}$

c) 1

d) None of these

15. Sum of infinite terms of the series

$$\cot^{-1}\left(1^2 + \frac{3}{4}\right) + \cot^{-1}\left(2^2 + \frac{3}{4}\right) + \cot^{-1}\left(3^2 + \frac{3}{4}\right) + \dots$$

a)  $\frac{\pi}{4}$

b)  $\tan^{-1}(2)$

c)  $\tan^{-1} 3$

d) None of these

16.  $2 \tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{7}\right)$  is equal to

a)  $\left(\frac{49}{29}\right)$

b)  $\frac{\pi}{2}$

c)  $-\left(\frac{49}{29}\right)$

d)  $\frac{\pi}{4}$

17. The number of triplets  $(x, y, z)$  satisfying  $\sin^{-1} x + \cos^{-1} y + \sin^{-1} z = 2\pi$ , is

a) 0

b) 2

c) 1

d) Infinite

18. The value of  $\sin(\cot^{-1} x)$  is

a)  $\sqrt{1+x^2}$

b)  $x$

c)  $(1+x^2)^{-3/2}$

d)  $(1+x^2)^{-1/2}$

19. If  $\cos^{-1} x + \cos^{-1} y = \frac{\pi}{2}$  and  $\tan^{-1} x - \tan^{-1} y = 0$ , then  $x^2 + xy + y^2$  is equal to

a) 0

b)  $\frac{1}{\sqrt{2}}$

c)  $\frac{3}{2}$

d)  $\frac{1}{8}$

20. If  $-1 < x < 1$ , then  $\tan^{-1}\left(\frac{2x}{1-x^2}\right)$  equals

a)  $2 \tan^{-1} x$

b)  $-\pi + 2 \tan^{-1} x$

c)  $\pi + 2 \tan^{-1} x$

d) None of these

## Topic :-INVERSE TRIGONOMETRIC FUNCTIONS

- If  $\theta = \tan^{-1} a$ ,  $\phi = \tan^{-1} b$  and  $ab = -1$ , then  $(\theta - \phi)$  is equal to  
 a) 0                                      b)  $\frac{\pi}{4}$                                       c)  $\frac{\pi}{2}$                                       d) None of these
- If the  $(\cos^{-1} x) = \sin\left(\cot^{-1} \frac{1}{2}\right)$ , then  $x$  is equal to  
 a)  $\pm \frac{5}{3}$                                       b)  $\pm \frac{\sqrt{5}}{3}$                                       c)  $\pm \frac{5}{\sqrt{3}}$                                       d) None of these
- If  $\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \pi$ , then  $x^4 + y^4 + z^4 + 4x^2y^2z^2 = k(x^2y^2 + y^2z^2 + z^2x^2)$   
 Where  $k$  is equal to  
 a) 1                                      b) 2                                      c) 4                                      d) none of these
- $\tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right) - \tan^{-1}\left(\frac{2x}{1-x^2}\right)$  is equal to  
 a) 0                                      b) 1                                      c)  $\tan^{-1} x$                                       d)  $\tan^{-1} 2x$
- If  $\cos^{-1} \sqrt{p} + \cos^{-1} \sqrt{1-p} + \cos^{-1} \sqrt{1-q} = \frac{3\pi}{4}$ , then the value of  $q$  is  
 a) 1                                      b)  $\frac{1}{\sqrt{2}}$                                       c)  $\frac{1}{3}$                                       d)  $\frac{1}{2}$
- If  $\alpha, \beta$  are the roots of the equation  $6x^2 - 5x + 1 = 0$ , then the value of  $\tan^{-1} \alpha + \tan^{-1} \beta$  is  
 a) 0                                      b)  $\pi/4$                                       c) 1                                      d)  $\pi/2$
- If  $\alpha = \sin^{-1} \frac{4}{5} + \sin^{-1} \frac{1}{3}$  and  $\beta = \cos^{-1} \frac{4}{5} + \cos^{-1} \frac{1}{3}$ , then  
 a)  $\alpha < \beta$                                       b)  $\alpha = \beta$                                       c)  $\alpha > \beta$                                       d) None of these
- Solution set of  $[\sin^{-1} x] > [\cos^{-1} x]$ , where  $[.]$  denote the greatest integer function, is  
 a)  $\left[\frac{1}{\sqrt{2}}, 1\right]$                                       b)  $(\cos 1, \sin 1)$                                       c)  $[\sin 1, 1]$                                       d) None of these
- The value of  $\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3$ , is  
 a) 0                                      b) 1                                      c)  $\pi$                                       d)  $-\pi$
- The greatest and the least values of  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3$  are respectively  
 a)  $-\frac{\pi}{2}, \frac{\pi}{2}$                                       b)  $-\frac{\pi^3}{8}, \frac{\pi^3}{8}$                                       c)  $\frac{\pi^3}{32}, \frac{7\pi^3}{8}$                                       d) None of these

11. If  $\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{3}{4}\right) - \tan^{-1}\left(\frac{x}{3}\right) = 0$ , then  $x$  is equal to  
 a)  $\frac{7}{3}$                       b) 3                      c)  $\frac{11}{3}$                       d)  $\frac{13}{3}$
12.  $\cos [\tan^{-1}\{\sin(\cot^{-1} x)\}]$  is equal to  
 a)  $\sqrt{\frac{x^2+2}{x^2+3}}$                       b)  $\sqrt{\frac{x^2+2}{x^2+1}}$                       c)  $\sqrt{\frac{x^2+1}{x^2+2}}$                       d) None of these
13.  $\tan^{-1} \frac{x}{y} - \tan^{-1} \frac{x-y}{x+y}$  is equal to  
 (where  $x < y > 0$ )  
 a)  $-\frac{\pi}{4}$                       b)  $\frac{\pi}{4}$                       c)  $\frac{3\pi}{4}$                       d) None of these
14. If  $\tan^{-1} 2$  and  $\tan^{-1} 3$  are two angles of a triangle, then the third angle is  
 a)  $\frac{\pi}{2}$                       b)  $\frac{\pi}{3}$                       c)  $\frac{\pi}{4}$                       d)  $\frac{\pi}{6}$
15. If  $\theta$  and  $\phi$  are the roots of the equation  $8x^2 + 22x + 5 = 0$ , then  
 a) Both  $\sin^{-1} \theta$  and  $\sin^{-1} \phi$  are equal                      b) Both  $\sec^{-1} \theta$  and  $\sec^{-1} \phi$  are equal  
 c) Both  $\tan^{-1} \theta$  and  $\tan^{-1} \phi$  are equal                      d) None of the above
16. If  $x_1, x_2, x_3, x_4$  are the roots of the equation  $x^4 - x^3 \sin 2\beta - x \cos \beta - \sin \beta = 0$ , then  
 $\tan^{-1} x_1 + \tan^{-1} x_2 + \tan^{-1} x_3 + \tan^{-1} x_4$  is equal to  
 a)  $\beta$                       b)  $\frac{\pi}{2} - \beta$                       c)  $\pi - \beta$                       d)  $-\beta$
17. The value of  $\cos(2 \cos^{-1} x + \sin^{-1} x)$  at  $x = \frac{1}{5}$  is  
 a) 1                      b) 3                      c) 0                      d)  $-\frac{2\sqrt{6}}{5}$
18. Solution of the equation  $\cot^{-1} x + \sin^{-1} \frac{1}{\sqrt{5}} = \frac{\pi}{4}$  is  
 a)  $x = 3$                       b)  $x = \frac{1}{\sqrt{5}}$                       c)  $x = 0$                       d) None of these
19. Let  $\cos(2 \tan^{-1} x) = \frac{1}{2}$ , then the value of  $x$  is  
 a)  $\sqrt{3}$                       b)  $\frac{1}{\sqrt{3}}$                       c)  $1 - \sqrt{3}$                       d)  $1 - \frac{1}{\sqrt{3}}$
20. If  $\sin^{-1} \frac{1}{3} + \sin^{-1} \frac{2}{3} = \sin^{-1} x$ , then the value of  $x$  is  
 a) 0                      b)  $\frac{(\sqrt{5}-4\sqrt{2})}{9}$                       c)  $\frac{(\sqrt{5}+4\sqrt{2})}{9}$                       d)  $\frac{\pi}{2}$

## Topic :-INVERSE TRIGONOMETRICE FUNCTIONS

- The solution set of the equation  $\tan^{-1} x - \cot^{-1} x = \cos^{-1}(2 - x)$  is  
 a)  $[0,1]$                       b)  $[-1,1]$                       c)  $[1,3]$                       d) None of these
- $\cos^{-1} \left\{ \frac{1}{2}x^2 + \sqrt{1-x^2} \sqrt{1-\frac{x^2}{4}} \right\} = \cos^{-1} \frac{x}{2} - \cos^{-1} x$  holds for  
 a)  $|x| \leq 1$                       b)  $x \in R$                       c)  $0 \leq x \leq 1$                       d)  $-1 \leq x \leq 0$
- The solutions of the equation  $\tan^{-1}(x+1) + \tan^{-1}(x-1) = \tan^{-1} \frac{8}{31}$  are  
 a)  $-\frac{1}{4}, 8$                       b)  $\frac{1}{4}, -8$                       c)  $-4, \frac{1}{8}$                       d)  $4, -\frac{1}{8}$
- If  $3 \sin^{-1} \frac{2x}{1+x^2} - 4 \cos^{-1} \frac{1+x}{1+x^2} + 2 \tan^{-1} \frac{2x}{1-x^2} = \frac{\pi}{3}$ , then value of  $x$  is  
 a)  $\sqrt{3}$                       b)  $\frac{1}{\sqrt{3}}$                       c) 1                      d) None of these
- If  $x^2 + y^2 + z^2 = r^2$ , then  $\tan^{-1} \left( \frac{xy}{zr} \right) + \tan^{-1} \left( \frac{yz}{xr} \right) + \tan^{-1} \left( \frac{xz}{yr} \right)$  is equal to  
 a)  $\pi$                       b)  $\frac{\pi}{2}$                       c) 0                      d) None of these
- The greatest and the least values of  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3$  are respectively  
 a)  $-\frac{\pi}{2}, \frac{\pi}{2}$                       b)  $-\frac{\pi^3}{8}, \frac{\pi^3}{8}$                       c)  $\frac{\pi^3}{32}, \frac{7\pi^3}{8}$                       d) None of these
- For the principle value branch of the graph of the function  $y = \sin^{-1} x, -1 \leq x \leq 1$ , which among the following is a true statement?  
 a) Graph is symmetric about the  $x$ -axis                      b) Graph is symmetric about the  $y$ -axis  
 c) Graph is not continuous                      d) The line  $x = 1$  is a tangent
- If  $-1 \leq x \leq -\frac{1}{\sqrt{2}}$ , then  $\sin^{-1}(2x\sqrt{1-x^2})$  equals  
 a)  $2 \sin^{-1} x$                       b)  $\pi - 2 \sin^{-1} x$                       c)  $-\pi - 2 \sin^{-1} x$                       d) None of these
- If  $a, b, c$  be positive real number and the value of  

$$\theta = \tan^{-1} \sqrt{\frac{a(a+b+c)}{bc}} + \tan^{-1} \sqrt{\frac{b(a+b+c)}{ca}} + \tan^{-1} \sqrt{\frac{c(c+b+c)}{ab}}$$

Then  $\tan \theta$  is equal to

- a) 0                      b) 1                      c)  $\frac{a+b+c}{abc}$                       d) None of these
10. If  $\theta \in [4\pi, 5\pi]$ , then  $\cos^{-1}(\cos \theta)$  equals  
 a)  $-4\pi + \theta$                       b)  $5\pi - \theta$                       c)  $4\pi - \theta$                       d)  $\theta - 5\pi$
11. The trigonometric equation  $\sin^{-1} x = 2 \sin^{-1} a$ , has a solution for  
 a)  $\frac{1}{2} < |a| < \frac{1}{\sqrt{2}}$                       b) All real values of  $a$                       c)  $|a| \leq \frac{1}{2}$                       d)  $|a| \geq \frac{1}{\sqrt{2}}$
12. The number of solutions of the equation  $\sin^{-1} x + \sin^{-1} 2x = \frac{\pi}{3}$ , is  
 a) 0                      b) 1                      c) 2                      d) Infinite
13. If  $2\sin^{-1} x = \sin^{-1}(2x\sqrt{1-x^2})$ , then  $x$  is equal to  
 a)  $[-1, 1]$                       b)  $[-\frac{1}{\sqrt{2}}, 1]$                       c)  $[-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}]$                       d) None of these
14. If  $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = \pi$ , then  
 a)  $x^2 + y^2 = z^2$                       b)  $x^2 + y^2 + z^2 = 0$   
 c)  $x^2 + y^2 + z^2 = 1 - 2xyz$                       d) None of the above
15. The value of  $\cot\left(\operatorname{cosec}^{-1}\frac{5}{3} + \tan^{-1}\frac{2}{3}\right)$  is  
 a)  $\frac{5}{17}$                       b)  $\frac{6}{17}$                       c)  $\frac{3}{17}$                       d)  $\frac{4}{17}$
16. If  $\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \pi$ , then  $x^4 + y^4 + z^4 + 4x^2y^2z^2 = k(x^2y^2 + y^2z^2 + z^2x^2)$   
 Where  $k$  is equal to  
 a) 1                      b) 2                      c) 4                      d) none of these
17. If  $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \pi$ , then the value of  $x + y + z$  is  
 a)  $-xyz$                       b)  $xyz$                       c)  $\frac{1}{xyz}$                       d) 0
18. The value of  $\cos^{-1}(\cos 12) - \sin^{-1}(\sin 14)$  is  
 a) 2                      b)  $8\pi - 26$                       c)  $4\pi + 2$                       d) None of these
19. If  $\frac{1}{2} \leq x \leq 1$ , then  $\sin^{-1}(3x - 4x^3)$  equals  
 a)  $3 \sin^{-1} x$                       b)  $\pi - 3 \sin^{-1} x$                       c)  $-\pi - 3 \sin^{-1} x$                       d) None of these
20. The value of  $\sin^{-1}\{\cos(4095^\circ)\}$  is equal to  
 a)  $-\frac{\pi}{3}$                       b)  $\frac{\pi}{6}$                       c)  $-\frac{\pi}{4}$                       d)  $\frac{\pi}{4}$

## Topic :- INVERSE TRIGONOMETRIC FUNCTIONS

1.  $\tan^{-1}\left(\frac{1}{4}\right) + \tan^{-1}\left(\frac{2}{9}\right) =$   
 a)  $\frac{1}{2} \cos^{-1}\left(\frac{3}{5}\right)$       b)  $\frac{1}{2} \sin^{-1}\left(\frac{3}{5}\right)$       c)  $\frac{1}{2} \tan^{-1}\left(\frac{3}{5}\right)$       d)  $\tan^{-1}\left(\frac{1}{2}\right)$
2. If  $\sin^{-1} \alpha + \sin^{-1} \beta + \sin^{-1} \gamma = \frac{3\pi}{2}$ , then  $\alpha\beta + \alpha\gamma + \beta\gamma$  is equal to  
 a) 1      b) 0      c) 3      d) -3
3. If  $A = \tan^{-1}\left(\frac{x\sqrt{3}}{2k-x}\right)$  and  $B = \tan^{-1}\left(\frac{2x-k}{k\sqrt{3}}\right)$ , then the value of  $A - B$  is  
 a)  $10^\circ$       b)  $45^\circ$       c)  $60^\circ$       d)  $30^\circ$
4. If in a  $\Delta ABC$ ,  $\angle A = \tan^{-1} 2$  and  $\angle B = \tan^{-1} 3$ , then angle  $C$  is equal to  
 a)  $\frac{\pi}{2}$       b)  $\frac{\pi}{3}$       c)  $\frac{\pi}{4}$       d) None of these
5. If  $(\tan^{-1} x)^2 + (\cot^{-1} x)^2 = \frac{5\pi^2}{8}$ , then  $x$  equals  
 a) -1      b) 1      c) 0      d) None of these
6.  $4 \tan^{-1} \frac{1}{5} - \tan^{-1} \frac{1}{239}$  is equal to  
 a)  $\pi$       b)  $\frac{\pi}{2}$       c)  $\frac{\pi}{3}$       d)  $\frac{\pi}{4}$
7. If  $\sin^{-1} x - \cos^{-1} x = \frac{\pi}{6}$ , then  $x$  is  
 a)  $\frac{1}{2}$       b)  $\frac{\sqrt{3}}{2}$       c)  $-\frac{1}{2}$       d) None of these
8. If the mapping  $f(x) = ax + b$ ,  $a > 0$  maps  $[-1, 1]$  onto  $[0, 2]$  then  $\cot[\cot^{-1} 7 + \cot^{-1} 8 + \cot^{-1} 18]$  is equal to  
 a)  $f(-1)$       b)  $f(0)$       c)  $f(1)$       d)  $f(2)$
9. The value of  $\sin^{-1}\left(\cos \frac{33\pi}{5}\right)$  is  
 a)  $\frac{3\pi}{5}$       b)  $\frac{7\pi}{5}$       c)  $\frac{\pi}{10}$       d)  $-\frac{\pi}{10}$
10. For the equation  $\cos^{-1} x + \cos^{-1} 2x + \pi = 0$ , then the number of real solutions is  
 a) 1      b) 2      c) 0      d)  $\infty$

11. The value of  $\tan \left\{ \frac{1}{2} \cos^{-1} \left( \frac{\sqrt{5}}{3} \right) \right\}$ , is  
 a)  $\frac{3+\sqrt{5}}{2}$       b)  $3 + \sqrt{5}$       c)  $\frac{1}{2}(3 - \sqrt{5})$       d) None of these
12. The value of  $\sin \left[ 2 \cos^{-1} \frac{\sqrt{5}}{3} \right]$  is  
 a)  $\frac{\sqrt{5}}{3}$       b)  $\frac{2\sqrt{5}}{3}$       c)  $\frac{4\sqrt{5}}{9}$       d)  $\frac{2\sqrt{5}}{9}$
13. If  $x > -\frac{1}{\sqrt{3}}$ , then  $\tan^{-1} \left( \frac{3x-x^3}{1-3x^2} \right)$  equals  
 a)  $3 \tan^{-1} x$       b)  $-\pi + 3 \tan^{-1} x$       c)  $\pi + 3 \tan^{-1} x$       d) None of these
14.  $\cos^{-1} \left( \frac{1}{2} \right) + 2 \sin^{-1} \left( \frac{1}{2} \right)$  is equal to  
 a)  $\frac{\pi}{6}$       b)  $\frac{\pi}{3}$       c)  $\frac{2\pi}{3}$       d)  $\frac{\pi}{4}$
15. If  $\sin \left( \sin^{-1} \frac{1}{5} + \cos^{-1} x \right) = 1$ , then the value of  $x$  is  
 a) -1      b)  $2/5$       c)  $1/3$       d)  $1/5$
16. If  $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = 3\pi$ , then  $xy + yz + zx$  is equal to  
 a) 0      b) 1      c) 3      d) -3
17. If  $0 \leq x < \infty$ , then  $\cos^{-1} \left( \frac{1-x^2}{1+x^2} \right)$  equals  
 a)  $2 \tan^{-1} x$       b)  $-2 \tan^{-1} x$       c)  $\pi - 2 \tan^{-1} x$       d)  $\pi + 2 \tan^{-1} x$
18. The value of  $\cos[2 \tan^{-1}(-7)]$  is  
 a)  $\frac{49}{50}$       b)  $-\frac{49}{50}$       c)  $\frac{24}{25}$       d)  $-\frac{24}{25}$
19. The value of  $\sin \left( 4 \tan^{-1} \frac{1}{3} \right) - \cos \left( 2 \tan^{-1} \frac{1}{7} \right)$  is  
 a)  $\frac{3}{7}$       b)  $\frac{7}{8}$       c)  $\frac{8}{21}$       d) None of these
20. If  $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = 3\pi$ , then  $xy + yz + zx$  is equal to  
 a) 0      b) 1      c) 3      d) -3

## Topic :-INVERSE TRIGONOMETRIC FUNCTIONS

- If  $a_1, a_2, a_3, \dots, a_n$  are in AP with common ratio  $d$ , then  $\tan \left[ \tan^{-1} \frac{d}{1+a_1a_2} + \tan^{-1} \frac{d}{1+a_2a_3} + \dots + \tan^{-1} \frac{d}{1+a_{n-1}a_n} \right]$  is equal to

a)  $\frac{(n-1)d}{a_1+a_n}$       b)  $\frac{(n-1)d}{1+a_1a_n}$       c)  $\frac{nd}{1+a_1a_n}$       d)  $\frac{a_n-a_1}{a_n+a_1}$
- $\sin \left( 2 \sin^{-1} \sqrt{\frac{63}{65}} \right)$  is equal to

a)  $\frac{2\sqrt{126}}{65}$       b)  $\frac{4\sqrt{65}}{65}$       c)  $\frac{8\sqrt{63}}{65}$       d)  $\frac{\sqrt{63}}{65}$
- If  $\sin^{-1} x - \cos^{-1} x = \frac{\pi}{6}$ , then  $x$  is

a)  $\frac{1}{2}$       b)  $\frac{\sqrt{3}}{2}$       c)  $-\frac{1}{2}$       d) None of these
- If  $\sin^{-1} \left( \frac{2x}{1+x^2} \right) + \cos^{-1} \left( \frac{1-x^2}{1+x^2} \right) = 4 \tan^{-1} x$ , then

a)  $x \in (-\infty, -1)$       b)  $x \in (1, \infty)$       c)  $x \in [0, 1]$       d)  $x \in [-1, 0]$
- $\tan^{-1} \frac{c_1x-y}{c_1y+x} + \tan^{-1} \frac{c_2-c_1}{1+c_2c_1} + \tan^{-1} \frac{c_3-c_2}{1+c_3c_2} + \dots + \tan^{-1} \frac{1}{c_n}$  is equal to

a)  $\tan^{-1} \frac{y}{x}$       b)  $\tan^{-1} yx$       c)  $\tan^{-1} \frac{x}{y}$       d)  $\tan^{-1}(x-y)$
- If  $\tan^{-1} a + \tan^{-1} b = \sin^{-1} 1 - \tan^{-1} c$ , then

a)  $a + b + c = abc$   
b)  $ab + bc + ca = abc$   
c)  $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} - \frac{1}{abc} = 0$   
d)  $ab + bc + ca = a + b + c$
- The value of  $\cos[\tan^{-1}\{\sin(\cot^{-1} x)\}]$  is

a)  $\sqrt{\frac{x^2+1}{x^2-1}}$       b)  $\sqrt{\frac{1-x^2}{x^2+2}}$       c)  $\sqrt{\frac{1-x^2}{1+x^2}}$       d)  $\sqrt{\frac{x^2+1}{x^2+2}}$
- If  $[\cot^{-1} x] + [\cos^{-1} x] = 0$ , where  $x$  is a non-negative real number and  $[.]$  denotes the greatest integer function, then complete set of values of  $x$  is

a)  $(\cos 1, 1] \cup b)$       (cot 1, 1)c)      (cos 1, cot 1)d)      None of these

9. If  $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = 3\pi$ , then  $xy + yz + zx$  is equal to  
a) 1                                      b) 0                                      c) -3                                      d) 3
10. A solution of the equation  $\tan^{-1}(1+x) + \tan^{-1}(1-x) = \frac{\pi}{2}$ , is  
a)  $x = 1$                                       b)  $x = -1$                                       c)  $x = 0$                                       d)  $x = \pi$
11.  $\tan\left(\frac{\pi}{4} + \frac{1}{2}\cos^{-1} x\right) + \tan\left(\frac{\pi}{4} - \frac{1}{2}\cos^{-1} x\right)$ ,  $x \neq 0$  is equal to  
a)  $x$                                       b)  $2x$                                       c)  $\frac{2}{x}$                                       d) None of these
12. The equation  $2\cos^{-1} x + \sin^{-1} x = \frac{11\pi}{6}$  has  
a) No solution                                      b) Only one solution                                      c) Two solutions                                      d) Three solutions
13. If  $\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \frac{3\pi}{2}$ , then the value of  $x^{100} + y^{100} + z^{100} - \frac{9}{x^{101} + y^{101} + z^{101}}$ , is  
a) 0                                      b) 1                                      c) 2                                      d) 3
14. If  $\sin\left(\sin^{-1}\frac{1}{5} + \cos^{-1} x\right) = 1$ , then  $x$  is equal to  
a) 1                                      b) 0                                      c)  $\frac{4}{5}$                                       d)  $\frac{1}{5}$
15. If the mapping  $f(x) = ax + b$ ,  $a > 0$  maps  $[-1, 1]$  onto  $[0, 2]$  then  $\cot[\cot^{-1} 7 + \cot^{-1} 8 + \cot^{-1} 18]$  is equal to  
a)  $f(-1)$                                       b)  $f(0)$                                       c)  $f(1)$                                       d)  $f(2)$
16. If  $\sin^{-1}\frac{2a}{1+a^2} - \cos^{-1}\frac{1-b^2}{1+b^2} = \tan^{-1}\frac{2x}{1-x^2}$ , then value of  $x$  is  
a)  $a$                                       b)  $b$                                       c)  $\frac{a+b}{1-ab}$                                       d)  $\frac{a-b}{1+ab}$
17. The sum of the two angles  $\cot^{-1} 3$  and  $\operatorname{cosec}^{-1}\sqrt{5}$ , is  
a)  $\frac{\pi}{2}$                                       b)  $\frac{\pi}{3}$                                       c)  $\frac{\pi}{4}$                                       d)  $\frac{\pi}{6}$
18.  $\tan\left[\frac{1}{2}\sin^{-1}\left(\frac{2a}{1+a^2}\right) + \frac{1}{2}\cos^{-1}\left(\frac{1-a^2}{1+a^2}\right)\right]$  is equal to  
a)  $\frac{2a}{1+a^2}$                                       b)  $\frac{1-a^2}{1+a^2}$                                       c)  $\frac{2a}{1-a^2}$                                       d) None of these
19. If  $\tan^{-1} x + \tan^{-1} y = \frac{\pi}{4}$ , then  
a)  $x + y + xy = 1$                                       b)  $x + y - xy = 1$   
c)  $x + y + xy + 1 = 0$                                       d)  $x + y - xy + 1 = 0$
20. If  $0 \leq x \leq 1$ , then  $\cos^{-1}(2x^2 - 1)$  equals  
a)  $2\cos^{-1} x$                                       b)  $\pi - 2\cos^{-1} x$                                       c)  $2\pi - 2\cos^{-1} x$                                       d) None of these

## Topic :-INVERSE TRIGONOMETRIC FUNCTIONS

1. If  $a, b, c$  be positive real number and the value of

$$\theta = \tan^{-1} \sqrt{\frac{a(a+b+c)}{bc}} + \tan^{-1} \sqrt{\frac{b(a+b+c)}{ca}} + \tan^{-1} \sqrt{\frac{c(c+b+c)}{ab}}$$

Then  $\tan \theta$  is equal to

- a) 0                                      b) 1                                      c)  $\frac{a+b+c}{abc}$                                       d) None of these
2. If  $\sin^{-1} x + \sin^{-1} y = \frac{\pi}{2}$ , then  $\cos^{-1} x + \cos^{-1} y$  is equal to  
 a)  $\frac{\pi}{2}$                                       b)  $\frac{\pi}{4}$                                       c)  $\pi$                                       d)  $\frac{3\pi}{4}$
3.  $\tan^{-1} \frac{c_1 x - y}{c_1 y + x} + \tan^{-1} \frac{c_2 - c_1}{1 + c_2 c_1} + \tan^{-1} \frac{c_3 - c_2}{1 + c_3 c_2} + \dots + \tan^{-1} \frac{1}{c_n}$  is equal to  
 a)  $\tan^{-1} \frac{y}{x}$                                       b)  $\tan^{-1} yx$                                       c)  $\tan^{-1} \frac{x}{y}$                                       d)  $\tan^{-1}(x - y)$
4. The value of  $\cos\{\tan^{-1}(\tan 2)\}$ , is  
 a)  $\frac{1}{\sqrt{5}}$                                       b)  $-\frac{1}{\sqrt{5}}$                                       c)  $\cos 2$                                       d)  $-\cos 2$
5. If  $\tan^{-1} \frac{x-1}{x+2} + \tan^{-1} \frac{x+1}{x+2} = \frac{\pi}{4}$ , then  $x$  is equal to  
 a)  $\frac{1}{\sqrt{2}}$                                       b)  $-\frac{1}{\sqrt{2}}$                                       c)  $\pm \sqrt{\frac{5}{2}}$                                       d)  $\pm \frac{1}{2}$
6. The sum of series  
 $\tan^{-1} \frac{1}{1+1+1^2} + \tan^{-1} \frac{1}{1+2+2^2} + \tan^{-1} \frac{1}{1+3+3^2} + \dots$   
 is equal to  
 a)  $\frac{\pi}{4}$                                       b)  $\frac{\pi}{2}$                                       c)  $\frac{\pi}{3}$                                       d)  $\frac{\pi}{6}$
7. The value of 'a' for which  $ax^2 + \sin^{-1}(x^2 - 2x + 2) + \cos^{-1}(x^2 - 2x + 2) = 0$  has a real solution, is  
 a)  $-\frac{2}{\pi}$                                       b)  $\frac{2}{\pi}$                                       c)  $-\frac{\pi}{2}$                                       d)  $\frac{\pi}{2}$
8. If  $\tan^{-1} x - \tan^{-1} y = \tan^{-1} A$ , then  $A$  is equal to  
 a)  $x - y$                                       b)  $x + y$                                       c)  $\frac{x-y}{1+xy}$                                       d)  $\frac{x+y}{1-xy}$

9. If  $\tan^{-1}\left(\frac{a}{x}\right) + \tan^{-1}\left(\frac{b}{x}\right) = \frac{\pi}{2}$ , then  $x$  is equal to  
a)  $\sqrt{ab}$                       b)  $\sqrt{2ab}$                       c)  $2ab$                       d)  $ab$
10.  $\cos^{-1}\frac{1}{2} + 2\sin^{-1}\frac{1}{2}$  is equal to  
a)  $\frac{\pi}{4}$                       b)  $\frac{\pi}{6}$                       c)  $\frac{\pi}{3}$                       d)  $\frac{2\pi}{3}$
11.  $4\tan^{-1}\frac{1}{5} - \tan^{-1}\frac{1}{239}$  is equal to  
a)  $\pi$                       b)  $\pi/2$                       c)  $\pi/3$                       d)  $\pi/4$
12. If  $2\sin^{-1}x = \sin^{-1}(2x\sqrt{1-x^2})$ , then  $x$  is equal to  
a)  $[-1,1]$                       b)  $\left[-\frac{1}{\sqrt{2}}, 1\right]$                       c)  $\left[-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right]$                       d) None of these
13. The value of  $\cot\left(\operatorname{cosec}^{-1}\frac{5}{3} + \tan^{-1}\frac{2}{3}\right)$ , is  
a)  $\frac{4}{17}$                       b)  $\frac{5}{17}$                       c)  $\frac{6}{17}$                       d)  $\frac{3}{17}$
14. Two angles of a triangle are  $\cot^{-1}2$  and  $\cot^{-1}3$ . Then, the third angle is  
a)  $\frac{\pi}{4}$                       b)  $\frac{3\pi}{4}$                       c)  $\frac{\pi}{6}$                       d)  $\frac{\pi}{3}$
15. If  $e^{[\sin^2\alpha + \sin^4\alpha + \sin^6\alpha + \dots]\log_e 2}$  is a root of equation  $x^2 - 9x + 8 = 0$ , where  $0 < \alpha < \frac{\pi}{2}$ , then the principle value of  $\sin^{-1}\sin\left(\frac{2\pi}{3}\right)$  is  
a)  $\alpha$                       b)  $2\alpha$                       c)  $-\alpha$                       d)  $-2\alpha$
16. If  $\frac{1}{2} \leq x \leq 1$ , then  $\cos^{-1}(4x^3 - 3x)$  equals  
a)  $3\cos^{-1}x$                       b)  $2\pi - 3\cos^{-1}x$                       c)  $-2\pi - 3\cos^{-1}x$                       d) None of these
17. If  $\sin^{-1}(2x\sqrt{1-x^2}) - 2\sin^{-1}x = 0$ , then  $x$  belongs to the interval  
a)  $[-1, 1]$                       b)  $[-1/\sqrt{2}, 1/\sqrt{2}]$                       c)  $[-1, -1/\sqrt{2}]$                       d)  $[1/\sqrt{2}, 1]$
18. Solution set of  $[\sin^{-1}x] > [\cos^{-1}x]$ , where  $[.]$  denotes the greatest integer function, is  
a)  $\left[\frac{1}{\sqrt{2}}, 1\right]$                       b)  $(\cos 1, \sin 1)$                       c)  $[\sin 1, 1]$                       d) None of these
19. If  $[\sin^{-1}\cos^{-1}\sin^{-1}x] = 1$ , where  $[.]$  denotes the greatest integer function, then  $x$  belongs to the interval  
a)  $[\tan \sin \cos 1, \tan \sin \cos \sin 1]$                       b)  $(\tan \sin \cos 1, \tan \sin \cos \sin 1)$   
c)  $[-1, 1]$                       d)  $[\sin \cos \tan 1, \sin \cos \sin \tan 1]$
20. The solution of  $\tan^{-1}x + 2\cot^{-1}x = \frac{2\pi}{3}$  is  
a)  $-\frac{1}{\sqrt{3}}$                       b)  $\frac{1}{\sqrt{3}}$                       c)  $-\sqrt{3}$                       d)  $\sqrt{3}$

## Topic :-INVERSE TRIGONOMETRIC FUNCTIONS

- If  $x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ , then the value of  $\tan^{-1}\left(\frac{\tan x}{4}\right) + \tan^{-1}\left(\frac{3 \sin 2x}{5+3 \cos 2x}\right)$  is  
 a)  $\frac{x}{2}$                       b)  $2x$                       c)  $3x$                       d)  $x$
- If  $-\frac{1}{2} \leq x \leq \frac{1}{2}$ , then  $\sin^{-1}(3x - 4x^3)$  equals  
 a)  $3 \sin^{-1} x$                       b)  $\pi - 3 \sin^{-1} x$                       c)  $-\pi - 3 \sin^{-1} x$                       d) None of these
- If  $\tan \theta + \tan\left(\frac{\pi}{3} + \theta\right) + \tan\left(\frac{-\pi}{3} + \theta\right) = K \tan 3\theta$ , then the value of  $K$  is  
 a) 1                      b)  $1/3$                       c) 3                      d) none of these
- If  $-1 \leq x \leq 0$ , then  $\cos^{-1}(2x^2 - 1)$  equals  
 a)  $2 \cos^{-1} x$                       b)  $\pi - 2 \cos^{-1} x$                       c)  $2\pi - 2 \cos^{-1} x$                       d)  $-2 \cos^{-1} x$
- If  $\alpha = \sin^{-1} \frac{\sqrt{3}}{2} + \sin^{-1} \frac{1}{3}$ ,  $\beta = \cos^{-1} \frac{\sqrt{3}}{2} + \cos^{-1} \frac{1}{3}$ , then  
 a)  $\alpha > \beta$                       b)  $\alpha = \beta$                       c)  $\alpha < \beta$                       d)  $\alpha + \beta = 2\pi$
- If  $x \in [-1, 1]$ , then  $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$  equals  
 a)  $2 \tan^{-1} x$                       b)  $\pi - 2 \tan^{-1} x$                       c)  $-\pi - 2 \tan^{-1} x$                       d) None of these
- $\sin\left[3 \sin^{-1}\left(\frac{1}{5}\right)\right]$  is equal to  
 a)  $\frac{71}{125}$                       b)  $\frac{74}{125}$                       c)  $\frac{3}{5}$                       d)  $\frac{1}{2}$
- If  $\sum_{i=1}^{20} \sin^{-1} x_i = 10\pi$ , then  $\sum_{i=1}^{20} x_i$  is equal to  
 a) 20                      b) 10                      c) 0                      d) None of these
- The value of  $x$  for which  $\sin[\cot^{-1}(1+x)] = \cos(\tan^{-1} x)$  is  
 a)  $\frac{1}{2}$                       b) 1                      c) 0                      d)  $-\frac{1}{2}$
- $\tan\left[\frac{\pi}{2} + \frac{1}{2} \cos^{-1}\left(\frac{a}{b}\right)\right] + \tan\left[\frac{\pi}{4} - \frac{1}{2} \cos^{-1}\left(\frac{a}{b}\right)\right]$  is equal to  
 a)  $\frac{2a}{b}$                       b)  $\frac{2b}{a}$                       c)  $\frac{a}{b}$                       d)  $\frac{b}{a}$

11.  $\tan^{-1} \frac{x}{y} - \tan^{-1} \frac{x-y}{x+y}$  is equal to  
(where  $x < y > 0$ )  
a)  $-\frac{\pi}{4}$  b)  $\frac{\pi}{4}$  c)  $\frac{3\pi}{4}$  d) None of these
12. The value of 'a' for which  $ax^2 + \sin^{-1}(x^2 - 2x + 2) + \cos^{-1}(x^2 - 2x + 2) = 0$  has a real solution, is  
a)  $-\frac{2}{\pi}$  b)  $\frac{2}{\pi}$  c)  $-\frac{\pi}{2}$  d)  $\frac{\pi}{2}$
13.  $\cos^{-1}\left(\frac{-1}{2}\right) - 2\sin^{-1}\left(\frac{1}{2}\right) + 3\cos^{-1}\left(\frac{-1}{\sqrt{2}}\right) - 4\tan^{-1}(-1)$  equals  
a)  $\frac{19\pi}{12}$  b)  $\frac{35\pi}{12}$  c)  $\frac{47\pi}{12}$  d)  $\frac{43\pi}{12}$
14. If  $\theta = \sin^{-1} x + \cos^{-1} x - \tan^{-1} x$ ,  $1 \leq x < \infty$ , then the smallest interval in which  $\theta$  lies is  
a)  $\frac{\pi}{2} \leq \theta \leq \frac{3\pi}{4}$  b)  $0 \leq \theta \leq \frac{\pi}{4}$  c)  $-\frac{\pi}{4} \leq \theta \leq 0$  d)  $\frac{\pi}{4} \leq \theta \leq \frac{\pi}{2}$
15. If  $4\sin^{-1} x + \cos^{-1} x = \pi$ , then  $x$  is equal to  
a) 0 b)  $1/2$  c)  $-1/2$  d) 1
16. The value of  $\sin^{-1}\left(\cos \frac{33\pi}{5}\right)$  is  
a)  $\frac{3\pi}{5}$  b)  $\frac{7\pi}{5}$  c)  $\frac{\pi}{10}$  d)  $-\frac{\pi}{10}$
17. If  $a_1, a_2, a_3, \dots, a_n$  are in AP with common ratio  $d$ , then  
 $\tan\left[\tan^{-1} \frac{d}{1+a_1a_2} + \tan^{-1} \frac{d}{1+a_2a_3} + \dots + \tan^{-1} \frac{d}{1+a_{n-1}a_n}\right]$  is equal to  
a)  $\frac{(n-1)d}{a_1+a_n}$  b)  $\frac{(n-1)d}{1+a_1a_n}$  c)  $\frac{nd}{1+a_1a_n}$  d)  $\frac{a_n-a_1}{a_n+a_1}$
18. If  $\tan^{-1}\left(\frac{a}{x}\right) + \tan^{-1}\left(\frac{b}{x}\right) = \frac{\pi}{2}$ , then  $x$  is equal to  
a)  $\sqrt{ab}$  b)  $\sqrt{2ab}$  c)  $2ab$  d)  $ab$
19. If  $A = \tan^{-1} x$ ,  $x \in R$ , then the value of  $\sin 2A$  is  
a)  $\frac{2x}{1-x^2}$  b)  $\frac{2x}{\sqrt{1-x^2}}$  c)  $\frac{2x}{1+x^2}$  d)  $\frac{1-x^2}{1+x^2}$
20. The value of  $x$ , where  $x > 0$  and  $\tan\left\{\sec^{-1}\left(\frac{1}{x}\right)\right\} = \sin(\tan^{-1} 2)$  is  
a)  $\sqrt{5}$  b)  $\frac{\sqrt{5}}{3}$  c) 1 d)  $\frac{2}{3}$

## Topic :-INVERSE TRIGONOMETRICE FUNCTIONS

1. If  $a < \frac{1}{32}$ , then the number of solutions of  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3 = a\pi^3$ , is  
 a) 0                                      b) 1                                      c) 2                                      d) Infinite
2. If  $\sqrt{3} + i = (a + ib)(c + id)$ , then  $\tan^{-1}\left(\frac{b}{a}\right) + \tan^{-1}\left(\frac{d}{c}\right)$  has the value  
 a)  $\frac{\pi}{3} + 2n\pi, n \in I$                       b)  $n\pi + \frac{\pi}{6}, n \in I$                       c)  $n\pi - \frac{\pi}{3}, n \in I$                       d)  $2n\pi - \frac{\pi}{3}, n \in I$
3. If  $\tan^{-1} \frac{1-x}{1+x} = \frac{1}{2} \tan^{-1} x$ , then the value of x is  
 a)  $\frac{1}{2}$                                       b)  $\frac{1}{\sqrt{3}}$                                       c)  $\sqrt{3}$                                       d) 2
4. The sum of the infinite series  $\cot^{-1} 2 + \cot^{-1} 8 + \cot^{-1} 18 + \cot^{-1} 32 + \dots$  is  
 a)  $\pi$                                       b)  $\frac{\pi}{2}$                                       c)  $\frac{\pi}{4}$                                       d) None of these
5. If  $y = \cos^{-1}(\cos 10)$ , then y is equal to  
 a) 10                                      b)  $4\pi - 10$                                       c)  $2\pi + 10$                                       d)  $2\pi - 10$
6. The principle value of  $\sin^{-1} \tan\left(\frac{-5\pi}{4}\right)$  is  
 a)  $\frac{\pi}{4}$                                       b)  $-\frac{\pi}{4}$                                       c)  $\frac{\pi}{2}$                                       d)  $-\frac{\pi}{2}$
7. The value of  $\sum_{r=0}^{\infty} \tan^{-1}\left(\frac{1}{1+r+r^2}\right)$  is equal to  
 a)  $\frac{\pi}{2}$                                       b)  $\frac{3\pi}{4}$                                       c)  $\frac{\pi}{4}$                                       d) None of these
8. If  $-1 \leq x \leq -\frac{1}{2}$ , then  $\cos^{-1}(4x^3 - 3x)$  equals  
 a)  $3 \cos^{-1} x$                                       b)  $2\pi - 3 \cos^{-1} x$                                       c)  $-2\pi + 3 \cos^{-1} x$                                       d) None of these
9. If  $\tan^{-1} x - \tan^{-1} y = \tan^{-1} A$ , then A is equal to  
 a)  $x - y$                                       b)  $x + y$                                       c)  $\frac{x-y}{1+xy}$                                       d)  $\frac{x+y}{1-xy}$
10. If  $2 \tan^{-1}(\cos x) = \tan^{-1}(2 \operatorname{cosec} x)$ , then the value of x is  
 a)  $\frac{3\pi}{4}$                                       b)  $\frac{\pi}{4}$                                       c)  $\frac{\pi}{3}$                                       d) None of these

11. The number of real solution of  $\tan^{-1} \sqrt{x(x+1)} + \sin^{-1} \sqrt{x^2 + x + 1} = \frac{\pi}{2}$  is  
 a) 0                                      b) 1                                      c) 2                                      d)  $\infty$
12.  $\cos \left\{ \cos^{-1} \left( -\frac{1}{7} \right) + \sin^{-1} \left( -\frac{1}{7} \right) \right\} =$   
 a)  $-\frac{1}{3}$                                       b) 0                                      c)  $\frac{1}{3}$                                       d)  $\frac{4}{9}$
13. The number of triplets  $(x, y, z)$  satisfying  $\sin^{-1} x + \cos^{-1} y + \sin^{-1} z = 2\pi$ , is  
 a) 0                                      b) 2                                      c) 1                                      d) Infinite
14. If  $\sin^{-1}(1-x) - 2 \sin^{-1} x = \frac{\pi}{2}$ , then  $x$  equals  
 a)  $0, -\frac{1}{2}$                                       b)  $0, \frac{1}{2}$                                       c) 0                                      d) None of these
15.  $\cos^{-1} \left( \frac{15}{17} \right) + 2 \tan^{-1} \left( \frac{1}{5} \right) =$   
 a)  $\frac{\pi}{2}$                                       b)  $\cos^{-1} \left( \frac{171}{221} \right)$                                       c)  $\frac{\pi}{4}$                                       d) None of these
16. If  $x < 0$ , then  $\tan^{-1} \left( \frac{1}{x} \right)$  equals  
 a)  $\cot^{-1} x$                                       b)  $-\cot^{-1} x$                                       c)  $-\pi + \cot^{-1} x$                                       d)  $-\pi - \cot^{-1} x$
17. If  $\cos^{-1} \sqrt{p} + \cos^{-1} \sqrt{1-p} + \cos^{-1} \sqrt{1-q} = \frac{3\pi}{4}$ , then the value of  $q$  is  
 a) 1                                      b)  $\frac{1}{\sqrt{2}}$                                       c)  $\frac{1}{3}$                                       d)  $\frac{1}{2}$
18.  $\tan^{-1} \frac{m}{n} - \tan^{-1} \frac{m-n}{m+n}$  is equal to  
 a)  $\tan^{-1} \frac{n}{m}$                                       b)  $\tan^{-1} \frac{m+n}{m-n}$                                       c)  $\frac{\pi}{4}$                                       d)  $\tan^{-1} \left( \frac{1}{2} \right)$
19. The value of  $\sin \left[ \frac{\pi}{2} - \sin^{-1} \left( -\frac{\sqrt{3}}{2} \right) \right]$  is  
 a)  $\frac{\sqrt{3}}{2}$                                       b)  $-\frac{\sqrt{3}}{2}$                                       c)  $\frac{1}{2}$                                       d)  $-\frac{1}{2}$
20. If  $\cos^{-1} x > \sin^{-1} x$ , then  
 a)  $x < 0$                                       b)  $-1 < x < 0$                                       c)  $0 \leq x < \frac{1}{\sqrt{2}}$                                       d)  $-1 \leq x < \frac{1}{\sqrt{2}}$