

Topic :-LIMITS AND DERIVATIVES

- $\lim_{\theta \rightarrow \frac{\pi}{2}} \frac{\frac{\pi}{2} - \theta}{\cot \theta}$ is equal to
 a) 0 b) -1 c) 1 d) ∞
- $\lim_{x \rightarrow 0} \frac{a^x - b^x}{e^x - 1}$ is equal to
 a) $\log_e \left(\frac{a}{b} \right)$ b) $\log_e \left(\frac{b}{a} \right)$ c) $\log_e(ab)$ d) $\log_e(a + b)$
- $\lim_{x \rightarrow -\infty} \frac{2x-1}{\sqrt{x^2+2x+1}}$ is equal to
 a) 2 b) -2 c) 1 d) -1
- $\lim_{x \rightarrow 2} \frac{\sqrt{1+\sqrt{2+x}} - \sqrt{3}}{x-2}$ is equal to
 a) $\frac{1}{8\sqrt{3}}$ b) $\frac{1}{\sqrt{3}}$ c) $8\sqrt{3}$ d) $\sqrt{3}$
- $\lim_{x \rightarrow 0} \left\{ \frac{1}{x^3\sqrt{8+x}} - \frac{1}{2x} \right\}$ is equal to
 a) $\frac{1}{12}$ b) $\frac{-4}{3}$ c) $\frac{-16}{3}$ d) $\frac{-1}{48}$
- The value of $\lim_{x \rightarrow 0} \frac{a^x - b^x}{x}$, is
 a) $\log \left(\frac{a}{b} \right)$ b) $\log \left(\frac{b}{a} \right)$ c) $\log(ab)$ d) $-\log(ab)$
- $\lim_{x \rightarrow 1} \frac{\sum_{r=1}^n x^r - n}{x-1}$ is equal to
 a) $\frac{n}{x}$ b) $\frac{n(n+1)}{2}$ c) 1 d) 0
- The value of $\lim_{x \rightarrow 1} (\log_5 5x)^{\log_x 5}$ is
 a) 1 b) e c) -1 d) None of these
- $\lim_{x \rightarrow 0} \frac{e^{\tan x} - e^x}{\tan x - x} =$
 a) 1 b) e c) $e - 1$ d) 0
- The value of $\lim_{x \rightarrow \infty} \left(\frac{x^2 - 2x + 1}{x^2 - 4x + 2} \right)^x$, is

- a) e^2 b) e^{-2} c) e^6 d) None of these
11. If $\lim_{x \rightarrow 0} \frac{\log(x+a) - \log a}{x} + k \lim_{x \rightarrow e} \frac{\log x - 1}{x - e} = 1$, then the value of k is
a) $1 - \frac{1}{a}$ b) $e(1 - a)$ c) $e\left(1 - \frac{1}{a}\right)$ d) $e(1 + a)$
12. The value of $\lim_{x \rightarrow \infty} \frac{\sin x}{x}$, is
a) 1 b) 0 c) -1 d) None of these
13. $\lim_{x \rightarrow 0} x \log \sin x$ is equal to
a) 0 b) ∞
c) 1 d) Cannot be determined
14. $\lim_{x \rightarrow 0} \frac{d}{dx} \int \frac{1 - \cos x}{x^2} dx$ is equal to
a) 1 b) 0 c) $1/2$ d) None of these
15. $\lim_{x \rightarrow 0} \frac{1}{x} \left\{ \int_y^a e^{\sin^2 t} dt - \int_{x+y}^a e^{\sin^2 t} dt \right\}$ is equal to (where a is a constant)
a) $e^{\sin^2 y}$ b) $\sin 2y e^{\sin^2 y}$ c) 0 d) None of these
16. Let $f''(x)$ be continuous at $x = 0$ and $f''(0) = 4$. Then $\lim_{x \rightarrow 0} \frac{2f(x) - 3f(2x) + f(4x)}{x^2}$ is equal to
a) 11 b) 2 c) 12 d) None of these
17. If $\lim_{x \rightarrow 0} \frac{[(a-n)x - \tan x] \sin nx}{x^2} = 0$, where n is non-zero real number, then a is equal to
a) 0 b) $\frac{n+1}{n}$ c) n d) $n + \frac{1}{n}$
18. The values of a and b such that $\lim_{x \rightarrow 0} \frac{x(1+a \cos x) - b \sin x}{x^3} = 0$, are
a) $\frac{5}{2}, \frac{3}{2}$ b) $\frac{5}{2}, -\frac{3}{2}$ c) $-\frac{5}{2}, -\frac{3}{2}$ d) None of these
19. The value of $\lim_{x \rightarrow \infty} \left(\frac{x^2 - 2x + 1}{x^2 - 4x + 2} \right)^x$ is
a) e^2 b) e^{-2} c) e^6 d) None of these
20. The value of $\lim_{x \rightarrow 0} \frac{(1 - \cos 2x)}{x^2}$ is
a) Does not exist b) Infinite c) 0 d) 2

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- The value of $\lim_{x \rightarrow 0} \frac{1 + \sin x - \cos x + \log(1-x)}{x^3}$, is
a) $1/2$ b) $-1/2$ c) 0 d) 1
- $\lim_{x \rightarrow 0} \left\{ \frac{1 + \tan x}{1 + \sin x} \right\}^{\operatorname{cosec} x}$ is equal to
a) $\frac{1}{e}$ b) 1 c) e d) e^2
- $\lim_{x \rightarrow \frac{\pi}{6}} \frac{2 \sin^2 x + \sin x - 1}{2 \sin^2 x - 3 \sin x + 1}$ is equal to
a) 3 b) -3 c) 6 d) 0
- The value of $\lim_{x \rightarrow 0} \left(\frac{1+5x^2}{1+3x^2} \right)^{1/x^2}$ is
a) e^2 b) e c) $\frac{1}{e}$ d) $\frac{1}{e^2}$
- If $f(x) = \begin{cases} x, & x < 0 \\ 1, & x = 0 \\ x^2, & x > 0 \end{cases}$, then $\lim_{x \rightarrow 0} f(x)$ is
a) 0 b) 1 c) 2 d) Does not exist
- If x is a real number in $[0, 1]$, then the value of $\lim_{m \rightarrow \infty} \lim_{n \rightarrow \infty} [1 + \cos^{2m}(n! \pi x)]$ is given by
a) 2 or 1 according as x is rational or irrational
b) 1 or 2 according as x is rational or irrational
c) 1 for all x
d) 2 or 1 for all x
- $\lim_{x \rightarrow 1} (1 + \cos \pi x) \cot^2 \pi x$ is equal to
a) 1 b) -1 c) $1/2$ d) $-1/2$
- If $\lim_{x \rightarrow 0} \frac{(e^{kx} - 1) \sin kx}{x^2} = 4$, then k is equal to
a) 2 b) -2 c) ± 2 d) ± 4
- $\lim_{x \rightarrow 0} \frac{\log(1+x^3)}{\sin^3 x}$ is equal to
a) 0 b) 1 c) 3 d) None of these

10. If $l_1 = \lim_{x \rightarrow 2^+} (x + [x])$, $l_2 = \lim_{x \rightarrow 2^-} (2x - [x])$ and $l_3 = \lim_{x \rightarrow \pi/2} \frac{\cos x}{(x - \pi/2)}$, then
a) $l_1 < l_2 < l_3$ b) $l_2 < l_3 < l_1$ c) $l_3 < l_2 < l_1$ d) $l_1 < l_3 < l_2$
11. If $f(x) = \begin{cases} \frac{\sin(1+[x])}{[x]}, & \text{for } [x] \neq 0 \\ 0, & \text{for } [x] = 0 \end{cases}$
Where $[x]$ denotes the greatest integer not exceeding x , then $\lim_{x \rightarrow 0^-} f(x)$ is equal to
a) -1 b) 0 c) 1 d) 2
12. $\lim_{x \rightarrow 0} \frac{(1 - \cos 2x) \sin 5x}{x^2 \sin 3x}$ equals
a) 10/3 b) 3/10 c) 6/5 d) 5/6
13. If $f(x) = \frac{\sin(e^{x-2} - 1)}{\log(x-1)}$, then $\lim_{x \rightarrow 2} f(x)$ is given by
a) -2 b) -1 c) 0 d) 1
14. If $S_n = \sum_{k=1}^n a_k$ and $\lim_{n \rightarrow \infty} a_n = a$, then $\lim_{n \rightarrow \infty} \frac{S_{n+1} - S_n}{\sqrt{\sum_{k=1}^n k}}$ is equal to
a) 0 b) a c) $\sqrt{2} a$ d) $2a$
15. $\lim_{h \rightarrow 0} \frac{\sin \sqrt{x+h} - \sin \sqrt{x}}{h}$ is equal to
a) $\cos \sqrt{x}$ b) $1/(2 \sin \sqrt{x})$ c) $(\cos \sqrt{x})/2\sqrt{x}$ d) $\sin \sqrt{x}$
16. The value of $\lim_{x \rightarrow \frac{\pi}{2}} (\sin x)^{\tan x}$ is
a) 1 b) 0 c) e d) None of these
17. The value of $\lim_{n \rightarrow \infty} \cos\left(\frac{x}{2}\right) \cos\left(\frac{x}{4}\right) \cos\left(\frac{x}{8}\right) \dots \cos\left(\frac{x}{2^n}\right)$ is
a) $\frac{x}{\sin x}$ b) $\frac{x}{\cos x}$ c) $\frac{(\sin x)}{x}$ d) $\frac{(\cos x)}{x}$
18. The value of the limit $\lim_{x \rightarrow 1} \frac{\sin(e^{x-1} - 1)}{\log x}$ is
a) 0 b) e c) $\frac{1}{e}$ d) 1
19. If $l = \lim_{x \rightarrow -2} \frac{\tan \pi x}{x+2} + \lim_{x \rightarrow \infty} \left(1 + \frac{1}{x^2}\right)^x$, then which one of the following is not correct?
a) $l > 3$
b) $l > 4$
c) $l < 4$
d) l is a transcendental number
20. $\lim_{x \rightarrow 1} \frac{\sqrt{1 - \cos 2(x-1)}}{x-1}$
a) Exists and is equals $\sqrt{2}$
b) Exists and is equals $-\sqrt{2}$
c) Does not exist because $x - 1 \rightarrow 0$

d) Does not exist because left hand limit is not equal to right hand limit



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1. If $f'(2) = 2, f''(2) = 1$, then $\lim_{x \rightarrow 2} \frac{2x^2 - 4f'(x)}{x-2}$, is
a) 4 b) 0 c) 2 d) ∞
2. $\lim_{x \rightarrow \pi/4} \frac{\int_2^{\sec^2 x} f(t) dt}{x^2 - \pi^2/16}$ equals
a) $\frac{8}{\pi} f(2)$ b) $\frac{2}{\pi} f(2)$ c) $\frac{2}{\pi} f\left(\frac{1}{2}\right)$ d) $4f(2)$
3. If $f(a) = 2, f'(a) = 1, g(a) = 3, g'(a) = -1$, then $\lim_{x \rightarrow a} \frac{f(a)g(x) - f(x)g(a)}{x-a}$ is equal to
a) 6 b) 1 c) -1 d) -5
4. If $f(x) = \left(\frac{x^2+5x+3}{x^2+x+2}\right)^x$ then $\lim_{x \rightarrow \infty} f(x)$ is equal to
a) e^4 b) e^3 c) e^2 d) 24
5. $\lim_{x \rightarrow 0} \frac{\sin^{-1} x - x}{x^3 \cos x}$ is equal to
a) 1/2 b) 1/3 c) 1/6 d) 1/12
6. For $x > 0$, $\lim_{x \rightarrow 0} \left((\sin x)^{1/x} + \left(\frac{1}{x}\right)^{\sin x} \right)$ is
a) 0 b) -1 c) 1 d) 2
7. The value of $\lim_{x \rightarrow \infty} \left(\frac{3x-4}{3x+2} \right)^{\frac{x+1}{3}}$ is equal to
a) $e^{-1/3}$ b) $e^{-2/3}$ c) e^{-1} d) e^{-2}
8. $\lim_{x \rightarrow 0} \frac{1}{x} \sin^{-1} \left(\frac{2x}{1+x^2} \right)$ is equal to
a) -2 b) 0 c) 2 d) ∞
9. $\lim_{x \rightarrow 0} \frac{2 \sin^2 3x}{x^2}$ is equal to
a) 0 b) 1 c) 18 d) 36
10. $\lim_{x \rightarrow 0} \frac{a^x + a^{-x} - 2}{x^2}$ is equal to
a) $(\log a)^2$ b) $\log a$ c) 0 d) None of these

11. Let $f(x) = \begin{cases} 1, & \text{when } x \text{ is rational} \\ 0, & \text{when } x \text{ is irrational} \end{cases}$, then $\lim_{x \rightarrow 0} f(x)$ is
a) 0 b) 1 c) $\frac{1}{2}$ d) None of these
12. For $x \in \mathbb{R}$ $\lim_{x \rightarrow \infty} \left(\frac{x-3}{x+2}\right)^x$ is equal to
a) e b) e^{-1} c) e^{-5} d) e^5
13. The value of $\lim_{x \rightarrow \infty} x \cos\left(\frac{\pi}{4x}\right) \sin\left(\frac{\pi}{4x}\right)$, is
a) $\frac{\pi}{2}$ b) $\frac{\pi}{4}$ c) 1 d) None of these
14. The derivative of function $f(x)$ is $\tan^4 x$. If $f(x) = 0$, then $\lim_{x \rightarrow 0} \frac{f(x)}{x}$ is equal to
a) 1 b) 0 c) -1 d) None of these
15. Let $f(x) = \begin{cases} (1/2)\{g(x) + (x)\}\sin(x), & x \geq 1 \\ \sin x/x, & x < 1 \end{cases}$
Where $g(x) = \begin{cases} 1, & \text{if } x > 0 \\ -1, & \text{if } x < 0 \\ 0, & \text{if } x = 0 \end{cases}$ Then, $\lim_{x \rightarrow 1} f(x)$ is equal to
a) 0 b) 2 c) $\sin 1$ d) None of these
16. If $\lim_{x \rightarrow \infty} \left[\frac{x^3+1}{x^2+1} - (ax + b)\right] = 2$, then
a) $a = 1$ and $b = 1$ b) $a = 1$ and $b = -1$ c) $a = 1$ and $b = -2$ d) $a = 1$ and $b = 2$
17. If $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by

$$f(x) = \begin{cases} \frac{x-2}{x^2-3x+2}, & \text{if } x \in \mathbb{R} - \{1, 2\} \\ 2, & \text{if } x = 1 \\ 1, & \text{if } x = 2 \end{cases}$$

Then $\lim_{x \rightarrow 2} \frac{f(x)-f(2)}{x-2}$ is equal to
a) 0 b) -1 c) 1 d) $-\frac{1}{2}$
18. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a differentiable function such that $f(3) = 3, f'(3) = \frac{1}{2}$. Then, the value of
 $\lim_{x \rightarrow 3} \frac{\int_3^{f(x)} 2t^3 dt}{x-3}$ is
a) 25 b) 26 c) 27 d) None of these
19. Let $f(a) = g(a) = k$ and their n th derivatives $f^n(a), g^n(a)$ exist and are not equal for some n . Further if
 $\lim_{x \rightarrow a} \frac{f(a)g(x) - f(x)g(a)}{g(x) - f(x)} = 4$, then the value of k is equal to
a) 4 b) 2 c) 1 d) 0
20. The value of $\lim_{x \rightarrow 0} \frac{\sin x}{\sqrt{x^2}}$, is

a) 1

b) -1

c) 0

d) None of these



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- The value of $\lim_{h \rightarrow 0} \frac{(a+h)^2 \sin(a+h) - a^2 \sin a}{h}$, is
a) $2a \sin a + a^2 \cos a$ b) $2a \sin a - a^2 \cos a$ c) $2a \cos a + a^2 \sin a$ d) None of these
- If $f(x)$ is differentiable function and $f''(0) = a$, then $\lim_{x \rightarrow 0} \frac{2f(x) - 3f(2x) + f(4x)}{x^2}$ is equal to
a) $3a$ b) $2a$ c) $5a$ d) $4a$
- The value of $\lim_{x \rightarrow 0} \frac{e^x + \log(1+x) - (1-x)^{-2}}{x^2}$ is equal to
a) 0 b) -3 c) -1 d) Infinity
- If for some real number k
 $\lim_{x \rightarrow 0} kx \operatorname{cosec}(x) = \lim_{x \rightarrow 0} x \operatorname{cosec}(kx)$, then the possible values of k are
a) $1, -1$ b) $0, 1$ c) $1, 2$ d) $0, \pi$
- The value of $\lim_{x \rightarrow 0} \frac{|x|}{x}$ is
a) 1 b) -1 c) 0 d) None of these
- $\lim_{x \rightarrow 0} x^2 \sin \frac{\pi}{x}$, is
a) 1 b) 0 c) Non-existent d) ∞
- The value of $\lim_{x \rightarrow \infty} \left(\frac{x^2 + bx + 4}{x^2 + ax + 5} \right)$ is
a) $\frac{b}{a}$ b) 0 c) 1 d) $\frac{4}{5}$
- If $f(x)$ is the integral function of the function $\frac{2 \sin x - \sin 2x}{x^3}$, $x \neq 0$, then $\lim_{x \rightarrow 0} f'(x)$ is equal to
a) 0 b) 1 c) -1 d) None of these
- The value of $\lim_{x \rightarrow \infty} \left(\frac{3x-4}{3x+4} \right)^{\left(\frac{x+1}{3} \right)}$, is
a) $e^{-2/3}$ b) $e^{-1/3}$ c) e^{-2} d) e^{-1}
- $\lim_{x \rightarrow 0} \frac{(1+x)^8 - 1}{(1+x)^2 - 1}$ is equal to

- a) 8 b) 6 c) 4 d) 2
11. The value of $\lim_{x \rightarrow \pi/4} \frac{2\sqrt{2} - (\cos x + \sin x)^3}{1 - \sin 2x}$, is
a) $\frac{3}{\sqrt{2}}$ b) $\frac{\sqrt{2}}{3}$ c) $\frac{1}{\sqrt{2}}$ d) $\sqrt{2}$
12. $\lim_{x \rightarrow -\infty} (3x + \sqrt{9x^2 - x})$ equals
a) 1/3 b) 1/6 c) -1/6 d) -1/3
13. $\lim_{x \rightarrow 0} \frac{e^{5x} - e^{4x}}{x}$ is equal to
a) 1 b) 2 c) 4 d) 5
14. Let $L = \lim_{x \rightarrow 0} \frac{a - \sqrt{a^2 - x^2} - x^2/4}{x^4}$, $a > 0$. If L is finite, then
a) $a = 2, L = \frac{1}{64}$ b) $a = 1, L = \frac{1}{64}$ c) $a = 3, L = \frac{1}{32}$ d) $a = 1, L = \frac{1}{32}$
15. $\lim_{x \rightarrow 0} x \log_e(\sin x)$ is equal to
a) -1 b) $\log_e 1$ c) 1 d) None of these
16. The value of $\lim_{x \rightarrow 0^+} x^m (\log x)^n$, m, n, N is
a) 0 b) m/n c) mn d) n/m
17. The value of $\lim_{x \rightarrow \infty} \frac{\sqrt{1+x^4} - (1+x^2)}{x^2}$ is equal to
a) 0 b) -1 c) 2 d) None of these
18. $\lim_{x \rightarrow 0} (\operatorname{cosec} x)^{1/\log x}$ is equal to
a) 0 b) 1 c) $1/e$ d) None of these
19. If $f(1) = 2$ and $f'(1) = 1$, then value of $\lim_{x \rightarrow 1} \frac{2x - f(x)}{x - 1}$ is
a) -1 b) 0 c) 1 d) 2
20. The value of $\lim_{x \rightarrow 0} \frac{1 - \cos(1 - \cos x)}{x^4}$ is
a) $\frac{1}{2}$ b) $\frac{1}{4}$ c) $\frac{1}{6}$ d) $\frac{1}{8}$

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- The value of $\lim_{x \rightarrow \infty} x^{3/2} (\sqrt{x^3 + 1} - \sqrt{x^3 - 1})$, is
a) 1 b) -1 c) 0 d) None of these
- If $\lim_{x \rightarrow a} \frac{a^x - x^a}{x^x - a^a} = -1$, then a equal to
a) 1 b) 0 c) e d) $(1/e)$
- If $\lim_{x \rightarrow 0} \left\{ \frac{x^3 + 1}{x^2 + 1} - (ax + b) \right\} = 2$, then
a) $a = 1, b = 1$ b) $a = 1, b = 2$ c) $a = 1, b = -2$ d) None of these
- $\lim_{x \rightarrow 0} \frac{e^{x^2} - \cos x}{x^2}$ is equal to
a) 0 b) $\frac{1}{2}$ c) 1 d) $\frac{3}{2}$
- $\lim_{n \rightarrow \infty} \left(\frac{1^2}{1-n^3} + \frac{2^2}{1-n^3} + \dots + \frac{n^2}{1-n^3} \right)$ is equal to
a) $\frac{1}{3}$ b) $-\frac{1}{3}$ c) $\frac{1}{6}$ d) $-\frac{1}{6}$
- $\lim_{x \rightarrow \frac{\pi}{6}} \frac{\sin 2x}{\sin x}$ is equal to
a) $\sqrt{3}$ b) $\frac{1}{\sqrt{3}}$ c) 2 d) $\frac{1}{2}$
- The value of $\lim_{x \rightarrow 0} \frac{1 - \cos(1 - \cos x)}{x^4}$, is
a) $\frac{1}{8}$ b) $\frac{1}{2}$ c) $\frac{1}{4}$ d) None of these
- Let α and β be the roots of the equation $ax^2 + bx + c = 0$, where $1 < \alpha < \beta$. If $\lim_{x \rightarrow m} \frac{|ax^2 + bx + c|}{ax^2 + bx + c} = 1$, then
a) $a < 0$ and $\alpha < m < \beta$ b) $a > 0$ and $m > 1$ c) $a > 0$ and $m < 1$ d) All the above
- $\lim_{x \rightarrow 1} \frac{x^m - 1}{x^n - 1}$ is equal to
a) $\frac{n}{m}$ b) $\frac{m}{n}$ c) $\frac{2m}{n}$ d) $\frac{2n}{m}$

10. Let α and β be the distinct roots of $ax^2 + bx + c = 0$, then $\lim_{x \rightarrow \alpha} \frac{1 - \cos(ax^2 + bx + c)}{(x - \alpha)^2}$ is equal to
a) $\frac{1}{2}(\alpha - \beta)^2$ b) $-\frac{a^2}{2}(\alpha - \beta)^2$ c) 0 d) $\frac{a^2}{2}(\alpha - \beta)^2$
11. $\lim_{x \rightarrow 0} \left[\frac{2^x - 1}{\sqrt{1+x} - 1} \right]$ is equal to
a) $\log_e 2$ b) $\log_e \sqrt{2}$ c) $\log_e 4$ d) 2
12. $\lim_{x \rightarrow 0} \left(\frac{x}{\sqrt{1+x} - \sqrt{1-x}} \right)$ is equal to
a) 0 b) 1 c) 2 d) -1
13. If $\lim_{x \rightarrow 0} \frac{\log(3+x) - \log(3-x)}{x} = k$, the value of k is
a) 0 b) -1/3 c) 2/3 d) -2/3
14. If a, b, c, d are positive, then $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{a+bx} \right)^{c+dx} =$
a) $e^{d/b}$ b) $e^{c/a}$ c) $e^{(c+d)/a+b}$ d) e
15. The value of $\lim_{x \rightarrow 0} \left(\frac{\int_0^{x^2} \sec^2 t \, dt}{x \sin x} \right)$ is
a) 3 b) 2 c) 1 d) 0
16. $\lim_{x \rightarrow \infty} \frac{\sin x}{x}$ is equal to
a) ∞ b) 1 c) 0 d) Does not exist
17. $\lim_{x \rightarrow 0} \frac{x \cos x - \log(1+x)}{x^2}$ equals
a) 1/2 b) 0 c) 1 d) -1/2
18. Given that $\lim_{n \rightarrow \infty} \sum_{r=1}^n \frac{\log(r+n) - \log n}{n} = 2 \left(\log 2 - \frac{1}{2} \right)$, $\lim_{n \rightarrow \infty} \frac{1}{n^k} [(n+1)^k (n+2)^k \dots (n+n)^k]^{1/n}$, is
a) $\frac{4k}{e}$ b) $\sqrt[k]{\frac{4}{e}}$ c) $\left(\frac{4}{e} \right)^k$ d) $\left(\frac{e}{4} \right)^k$
19. $\lim_{x \rightarrow 0} \frac{\sin |x|}{x}$ is equal to
a) 1 b) 0 c) positive infinity d) does not exist
20. The value of $\lim_{x \rightarrow \infty} \left\{ \frac{x^2 \sin\left(\frac{1}{x}\right) - x}{1 - |x|} \right\}$, is
a) 0 b) 1 c) -1 d) None of these

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- If $l_1 = \lim_{x \rightarrow -2} (x + |x|)$, $l_2 = \lim_{x \rightarrow -2} (2x + |x|)$ and $l_3 = \lim_{x \rightarrow \pi/2} \frac{\cos x}{x - \pi/2}$, then
 a) $l_1 < l_2 < l_3$ b) $l_2 < l_3 < l_1$ c) $l_3 < l_2 < l_1$ d) $l_1 < l_3 < l_2$
- $\lim_{x \rightarrow \infty} \left(\frac{x+2}{x+1} \right)^{x+3}$ is equal to
 a) 1 b) e c) e^2 d) e^3
- $\lim_{x \rightarrow 0} \frac{1}{x^{12}} \left\{ 1 - \cos \frac{x^2}{2} - \cos \frac{x^4}{4} + \cos \frac{x^2}{2} \cos \frac{x^4}{4} \right\}$ is equal to
 a) $\frac{1}{32}$ b) $\frac{1}{256}$ c) $\frac{1}{16}$ d) $-\frac{1}{256}$
- If $f(x) = \sqrt{\frac{x - \sin x}{x + \cos^2 x}}$, then $\lim_{x \rightarrow \infty} f(x)$ is
 a) 0 b) ∞ c) 1 d) None of these
- The value of $\lim_{x \rightarrow 1} (2 - x)^{\tan \frac{\pi x}{2}}$ is equal to
 a) $e^{-2/\pi}$ b) $e^{1/\pi}$ c) $e^{2/\pi}$ d) $e^{-1/\pi}$
- $\lim_{n \rightarrow \infty} r^n = 0$, then r is equal to
 a) $\frac{4}{5}$ b) $\frac{5}{4}$ c) 2 d) 1
- The value of $\lim_{x \rightarrow 0} \frac{5^x - 5^{-x}}{2x}$ is
 a) $\log 5$ b) 0 c) 1 d) $2 \log 5$
- $\lim_{x \rightarrow 0} \frac{\sqrt{1 - \cos 2x}}{\sqrt{2x}}$ is
 a) λ b) -1 c) 0 d) Does not exist
- The value of $\lim_{x \rightarrow \infty} a^x \sin \left(\frac{b}{a^x} \right)$ is ($a > 1$)
 a) $b \log a$ b) $a \log b$ c) b d) None of these
- $\lim_{x \rightarrow \infty} \left(\frac{x^3}{3x^2 - 4} - \frac{x^2}{3x + 2} \right)$ is equal to
 a) $-\frac{1}{4}$ b) $-\frac{1}{2}$ c) 0 d) $\frac{2}{9}$

11. $\lim_{x \rightarrow 0} \frac{e^{x^2} - \cos x}{x^2}$ is equal to
a) $3/2$ b) $1/2$ c) $2/3$ d) None of these
12. The value of $\lim_{x \rightarrow \infty} \left\{ \frac{a_1^{1/x} + a_2^{1/x} + \dots + a_n^{1/x}}{n} \right\}^1$, is
a) $a_1 + a_2 + \dots + a_n$ b) $e^{a_1 + a_2 + \dots + a_n}$ c) $\frac{a_1 + a_2 + \dots + a_n}{n}$ d) $a_1 a_2 \dots a_n$
13. The value of $\lim_{x \rightarrow 0} \frac{\sin^2 x + \cos x - 1}{x^2}$ is
a) 1 b) $\frac{1}{2}$ c) $-\frac{1}{2}$ d) 0
14. $\lim_{x \rightarrow 0} \frac{\sin 4x}{1 - \sqrt{1-x}}$ is
a) 4 b) 8 c) 10 d) 2
15. $\lim_{x \rightarrow 1} \frac{x^8 - 2x + 1}{x^4 - 2x + 1}$ equals
a) 3 b) 0 c) -3 d) 1
16. The value of $\lim_{x \rightarrow \infty} \sqrt{a^2 x^2 + ax + 1} - \sqrt{a^2 x^2 + 1}$ is
a) $\frac{1}{2}$ b) 1 c) 2 d) None of these
17. $\lim_{x \rightarrow 0} (-1)^{[x]}$, where $[.]$ denotes the greatest integer function is equal to
a) 0 b) 1 c) -1 d) Does not exist
18. $\lim_{x \rightarrow 0} \frac{(1-e^x) \sin x}{x^2 + x^3}$ is equal to
a) -1 b) 0 c) 1 d) 2
19. The value of $\lim_{x \rightarrow \infty} \left(\frac{x+3}{x+1} \right)^{x+2}$ is
a) 0 b) 1 c) e^2 d) e^4
20. If α is a repeated root of $ax^2 + bx + c = 0$, then $\lim_{x \rightarrow \alpha} \frac{\sin(ax^2 + bx + c)}{(x-\alpha)^2}$ is
a) 0 b) a c) b d) c

Topic :-LIMITS AND DERIVATIVES

- The value of $\lim_{x \rightarrow 0} \frac{e^x - (1+x)}{x^2}$, is
a) 0 b) $1/2$ c) 2 d) e
- $\lim_{x \rightarrow \infty} \frac{(2x+1)^{40}(4x-1)^5}{(2x+3)^{45}}$ is equal to
a) 16 b) 24 c) 32 d) 8
- If $f: R \rightarrow R$ is defined by $f(x) = [x - 3] + [x - 4]$ for $x \in R$, then $\lim_{x \rightarrow 3^-} f(x)$ is equal to
a) -2 b) -1 c) 0 d) 1
- The value of $\lim_{x \rightarrow 2^-} \{x + (x - [x])^2\}$, is
a) 0 b) 1 c) 2 d) 3
- The value of $\lim_{x \rightarrow \infty} \left(\frac{x^2 + 2x + 3}{2x^2 + x + 5} \right)^{\frac{3x-2}{3x+2}}$, is
a) $e^{1/2}$ b) $e^{3/2}$ c) e^3 d) None of these
- $\lim_{x \rightarrow 0} \left[\frac{e^x - e^{\sin x}}{x - \sin x} \right]$ is equal to
a) -1 b) 0 c) 1 d) None of these
- The value of $\lim_{x \rightarrow 1} (\log_2 2x)^{\log_x 5}$ is
a) $5/2$ b) $e^{\log_2 5}$ c) $\log 5 / \log 2$ d) $e^{\log_5 2}$
- Let $f: R \rightarrow R$ be appositive increasing function with $\lim_{x \rightarrow \infty} \frac{f(3x)}{f(x)} = 1$. Then, $\lim_{x \rightarrow \infty} \frac{f(2x)}{f(x)}$ is equal to
a) 1 b) $\frac{2}{3}$ c) $\frac{3}{2}$ d) 3
- If $f(x) = \begin{cases} x^2 - 3, & 2 < x < 3 \\ 2x + 5, & 3 < x < 4 \end{cases}$, the equation whose roots are $\lim_{x \rightarrow 3^-} f(x)$ and $\lim_{x \rightarrow 3^+} f(x)$, is
a) $x^2 - 7x + 3 = 0$ b) $x^2 - 20x + 66 = 0$ c) $x^2 - 17x + 66 = 0$ d) $x^2 - 18x + 60 = 0$
- If $f(x) = \begin{cases} x \sin\left(\frac{1}{x}\right), & x \neq 0 \\ 0, & x = 0 \end{cases}$ Then, $\lim_{x \rightarrow 0} f(x)$
a) Is equal to 1 b) Is equal to -1 c) Is equal to 0 d) Does not exist

11. The value of $\lim_{x \rightarrow -\pi} \frac{|x+\pi|}{\sin x}$
 a) Is equal to -1 b) Is equal to 1 c) Is equal to π d) Does not exist
12. Let $f(x) = \frac{1}{\sqrt{18-x^2}}$. The value of $\lim_{x \rightarrow 3} \frac{f(x)-f(3)}{x-3}$, is
 a) 0 b) $-\frac{1}{9}$ c) $-\frac{1}{3}$ d) $\frac{1}{9}$
13. The value of $\lim_{x \rightarrow \infty} \frac{5^{x+1}-7^{x+1}}{5^x-7^x}$, is
 a) 5 b) -5 c) 7 d) -7
14. If $A_i = \frac{x-a_i}{|x-a_i|}$, $i = 1, 2, \dots, n$ and if $a_1 < a_2 < a_3 < \dots < a_n$. Then, $\lim_{x \rightarrow a_m} (A_1 A_2 \dots A_n)$, $1 \leq m \leq n$
 a) Is equal to $(-1)^m$ b) Is equal to $(-1)^{m+1}$ c) Is equal to $(-1)^{m-1}$ d) Does not exist
15. $\lim_{x \rightarrow -1} \frac{(1+x)(1-x^2)(1+x^3)(1-x^4)\dots(1-x^{4n})}{[(1+x)(1-x^2)(1+x^3)(1-x^4)\dots(1-x^{2n})]^2}$ is equal to
 a) ${}^{4n}C_{2n}$ b) ${}^{2n}C_n$ c) $2 \cdot {}^{4n}C_{2n}$ d) $2 \cdot {}^{4n}C_n$
16. The value of $\lim_{x \rightarrow \infty} \frac{\log x}{x^n}$, $n > 0$ is
 a) 0 b) 1 c) $\frac{1}{n}$ d) $\frac{1}{n!}$
17. If f be a function such that $f(9) = 9$ and $f'(9) = 3$, then $\lim_{x \rightarrow 9} \frac{\sqrt{f(x)}-3}{\sqrt{x}-3}$ is equal to
 a) 9 b) 3 c) 1 d) None of these
18. Let $f(x) = \lim_{n \rightarrow \infty} \frac{x^{2n}-1}{x^{2n}+1}$, then
 a) $f(x) = \begin{cases} 1, & |x| > 1 \\ -1, & |x| < 1 \end{cases}$
 b) $f(x) = \begin{cases} 1, & |x| < 1 \\ -1, & |x| > 1 \end{cases}$
 c) $f(x)$ is not defined for any value of x
 d) $f(x) = 1$ for $|x| = 1$
19. $\lim_{x \rightarrow 1} \frac{e^{-x}-e^{-1}}{x-1}$ is equal to
 a) $\frac{1}{e}$ b) $-\frac{1}{e}$ c) 1 d) None of these
20. The value of $\lim_{n \rightarrow \infty} \frac{x^n}{x^{n+1}}$, where $x < -1$ is
 a) $\frac{1}{2}$ b) $-\frac{1}{2}$ c) 1 d) None of these

Topic :-LIMITS AND DERIVATIVES

- If $a = \min\{x^2 + 4x + 5 : x \in R\}$ and $b = \lim_{\theta \rightarrow 0} \frac{1 - \cos 2\theta}{\theta^2}$, then the value of $\sum_{r=0}^n {}^nC_r a^r b^{n-r}$, is
a) $2n$ b) 3^n c) 2^{n+1} d) 2^{n-1}
- If $0 < x < y$, then $\lim_{n \rightarrow \infty} (y^n + x^n)^{1/n}$ is equal to
a) e b) x c) y d) None of these
- $\lim_{x \rightarrow 1} (\log ex)^{1/\log x}$ is equal to
a) e^{-1} b) e c) e^2 d) 0
- If $\lim_{x \rightarrow \infty} \left\{ ax - \frac{x^2+1}{x+1} \right\} = b$, a finite number, then
a) $a = 1, b = 1$ b) $a = 0, b = 1$ c) $a = -1, b = 1$ d) $b = -1, a = -1$
- The value of $\lim_{x \rightarrow 0} \frac{1}{x^3} \int_0^x \frac{t \log(1+t)}{t^4+4} dt$ is
a) 0 b) $\frac{1}{12}$ c) $\frac{1}{24}$ d) $\frac{1}{64}$
- For the function $f(x) = \lim_{n \rightarrow \infty} \frac{\log(2+x) + x^{2n} \sin x}{1+x^{2n}}$ Which of the following is true?
a) $\lim_{x \rightarrow 1^-} f(x)$ does not exist
b) $\lim_{x \rightarrow 1^+} f(x)$ does not exist
c) Both limits exist and $\lim_{x \rightarrow 1^-} f(x) = \lim_{x \rightarrow 1^+} f(x)$
d) Both limits exist and $\lim_{x \rightarrow 1^-} f(x) \neq \lim_{x \rightarrow 1^+} f(x)$
- $\lim_{x \rightarrow \infty} \frac{\int_0^{2x} x e^{x^2} dx}{e^{4x^2}}$ equals
a) 0 b) ∞ c) 2 d) $1/2$
- The value of $\lim_{x \rightarrow \pi/2} \tan^2 x (\sqrt{2 \sin^2 x + 3 \sin x + 4} - \sqrt{\sin^2 x + 6 \sin x + 2})$ is equal to
a) $\frac{1}{10}$ b) $\frac{1}{11}$ c) $\frac{1}{12}$ d) $\frac{1}{8}$

9. $\lim_{x \rightarrow \infty} \left(\frac{x+2}{x+1}\right)^{x+3}$ is
 a) 1 b) e c) e^2 d) e^3
10. If $f(x) = \cot^{-1}[(3x - x^3)/(1 - 3x^2)]$ and $g(x) = \cos^{-1}[(1 - x^2)/(1 + x^2)]$, then
 $\lim_{x \rightarrow a} \frac{f(x) - f(a)}{g(x) - g(a)} \left(0 < a < \frac{1}{2}\right)$ is
 a) $-\frac{3}{2}$ b) $\frac{1}{2}$ c) $\frac{3}{2}$ d) None of these
11. Let $f(x) = \begin{cases} x^2, & x \in \mathbb{Z} \\ \frac{k(x^2-4)}{2-x}, & x \notin \mathbb{Z} \end{cases}$ Then, $\lim_{x \rightarrow 2} f(x)$
 a) Exists only when $k = 1$
 b) Exists for every real k
 c) Exists for every real k except $k = 1$
 d) Does not exist
12. The value of $\lim_{x \rightarrow 0} \frac{1 - \cos^3 x}{x \sin x \cos x}$ is
 a) $2/5$ b) $3/5$ c) $3/2$ d) $3/4$
13. $\lim_{x \rightarrow \infty} \sqrt{\frac{x + \sin x}{x - \cos x}} =$
 a) 0 b) 1 c) -1 d) None of these
14. It is given that $f'(a)$ exists, then $\lim_{x \rightarrow a} \frac{xf(a) - af(x)}{x - a}$ is equal to
 a) $f(a) - af'(a)$ b) $f'(a)$ c) $-f'(a)$ d) $f(a) + af'(a)$
15. $\lim_{h \rightarrow 0} \frac{\sin(a+3h) - 3 \sin(a+2h) + 3 \sin(a+h) - \sin a}{h^3}$ is equal to
 a) $\sin a$ b) $-\sin a$ c) $\cos a$ d) $-\cos a$
16. $\lim_{x \rightarrow 0} \left\{ \frac{1^x + 2^x + 3^x + \dots + n^x}{n} \right\}^{1/x}$ is equal to
 a) $(n!)^n$ b) $(n!)^{1/n}$ c) $n!$ d) $\ln n!$
17. The value of $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \cos t^2 dt}{x \sin x}$ is
 a) $3/2$ b) 1 c) -1 d) None of these
18. If $f(x) = \frac{2}{x-3}$, $g(x) = \frac{x-3}{x+4}$ and $h(x) = -\frac{2(2x+1)}{x^2+x-12}$, then $\lim_{x \rightarrow 3} \{f(x) + g(x) + h(x)\}$, is
 a) -2 b) -1 c) $-2/7$ d) 0
19. $\lim_{x \rightarrow 0} \left[\frac{8 \sin x + x \cos x}{3 \tan x + x^2} \right]$ is equal to
 a) 3 b) 2 c) -1 d) 4

20. If $\lim_{x \rightarrow 0} \frac{\log(3+x) - \log(3-x)}{x} = k$, the value of k is

a) $-2/3$

b) 0

c) $-1/3$

d) $2/3$



[illegible]

- The value of $\lim_{x \rightarrow \infty} \left(\frac{x^2+6}{x^2-6} \right)^x$ is given by
 - 0
 - 1
 - 1
 - None of these
- $\lim_{x \rightarrow \infty} \left(\frac{x^2+5x+3}{x^2+x+2} \right)^x$ is equal to
 - e^4
 - e^2
 - e^3
 - e
- If $G(x) = \sqrt{25 - x^2}$, then $\lim_{x \rightarrow 1} \frac{G(x) - G(1)}{x - 1}$ has the value
 - $\frac{1}{\sqrt{24}}$
 - $\frac{1}{5}$
 - $-\sqrt{24}$
 - $-1/5$
- $\lim_{x \rightarrow 1} \cos^{-1} \left(\frac{1 - \sqrt{x}}{1 - x} \right)$ is equal to
 - $\frac{\pi}{3}$
 - $\frac{\pi}{6}$
 - $\frac{\pi}{2}$
 - $\frac{\pi}{4}$
- $\lim_{x \rightarrow 1} \frac{\sin(e^x - 1)}{\log x}$ is equal to
 - 1
 - 0
 - e
 - e^{-1}
- $\lim_{x \rightarrow \frac{\pi}{6}} \left[\frac{3 \sin x - \sqrt{3} \cos x}{6x - \pi} \right]$
 - $\sqrt{3}$
 - $\frac{1}{\sqrt{3}}$
 - $-\frac{1}{\sqrt{3}}$
 - $-\frac{1}{3}$
- Let $f: R \rightarrow R$ be a differentiable function such that $f(2) = 2$. Then, the value of $\lim_{x \rightarrow 2} \int_2^{f(x)} \frac{4t^3}{x-2} dt$, is
 - $6f'(2)$
 - $12f'(2)$
 - $32f'(2)$
 - None of these
- $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\int_2^{\sec^2 x} f(t) dt}{x^2 - \frac{\pi^2}{16}}$ equals
 - $\frac{8}{\pi} f(2)$
 - $\frac{2}{\pi} f(2)$
 - $\frac{2}{\pi} f\left(\frac{1}{2}\right)$
 - $4f(2)$
- If $f(x) = \sqrt{\frac{x - \sin x}{x + \cos^2 x}}$, then $\lim_{x \rightarrow \infty} f(x)$ is
 - 0
 - ∞
 - 1
 - None of these

10. Let $f(x)$ be twice differentiable function such that $f''(0) = 2$. Then, $\lim_{x \rightarrow 0} \frac{2f(x) - 3f(2x) + f(4x)}{x^2}$ is
 a) 6 b) 3 c) 12 d) None of these
11. The value of $\lim_{x \rightarrow \pi/2} \frac{\cot x - \cos x}{(\pi - 2x)^3}$
 a) 1 b) $\frac{1}{16}$ c) 16 d) None of these
12. The value of $\lim_{x \rightarrow \infty} \left(\frac{x+3}{x-1} \right)^{x+3}$, is
 a) e b) e^2 c) e^4 d) $1/e$
13. The value of $\lim_{x \rightarrow 7} \frac{2 - \sqrt{x-3}}{x^2 - 49}$ is
 a) $2/9$ b) $-2/49$ c) $1/64$ d) $-1/56$
14. $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2+1} - \sqrt[3]{x^3+1}}{\sqrt[4]{x^4+1} - \sqrt[5]{x^4+1}}$ equals
 a) 1 b) 0 c) -1 d) None of these
15. Let $f: R \rightarrow R$ be a differentiable function having $f(2) = 6, f'(2) = \left(\frac{1}{48}\right)$. Then, $\lim_{x \rightarrow 2} \frac{\int_6^{f(x)} 4t^3 dt}{x-2}$ is equals
 a) 18 b) 12 c) 36 d) 24
16. If $g(x)$ is a polynomial satisfying $g(x)g(y) = g(x) + g(y) + g(xy) - 2$ for all real x and y and $g(2) = 5$, then $\lim_{x \rightarrow 3} g(x)$ is
 a) 9 b) 10 c) 25 d) 20
17. $\lim_{x \rightarrow \pi/4} \frac{1 - \cot^3 x}{2 - \cot x - \cot^3 x}$, is
 a) $\frac{11}{4}$ b) $\frac{3}{4}$ c) $\frac{1}{2}$ d) None of these
18. If $[x]$ denotes the greatest integer less than or equal to x , then the value of $\lim_{x \rightarrow 1} \{1 - x + [x - 1] + [1 - x]\}$ is
 a) 0 b) 1 c) -1 d) None of these
19. If $\lim_{x \rightarrow 1} \frac{ax^2 + bx + c}{(x-1)^2} = 2$, then (a, b, c) is
 a) $(2, -4, 2)$ b) $(2, 4, 2)$ c) $(2, 4, -2)$ d) $(2, -4, -2)$
20. $\lim_{x \rightarrow 1} \frac{2x^2 + x - 3}{3x^3 - 3x^2 + 2x - 2}$ is equal to
 a) 1 b) 2 c) -1 d) -2

Topic :-LIMITS AND DERIVATIVES

- $\lim_{x \rightarrow \infty} (\sqrt{x + \sqrt{x + \sqrt{x}}} - \sqrt{x})$ is equal to
 a) $\frac{1}{2}$ b) 0 c) 1 d) None of these
- The value of $\lim_{x \rightarrow \infty} \left(\frac{x+6}{x+1}\right)^{x+4}$, is
 a) e b) e^2 c) e^4 d) e^5
- Let α and β be the roots of $ax^2 + bx + c = 0$, then $\lim_{x \rightarrow a} \frac{1 - \cos(ax^2 + bx + c)}{(x - \alpha)^2}$ is equal to
 a) 0 b) $\frac{1}{2}(\alpha - \beta)^2$ c) $\frac{a^2}{2}(\alpha - \beta)^2$ d) $-\frac{a^2}{2}(\alpha - \beta)^2$
- $\lim_{x \rightarrow 0} (1 - ax)^{1/x}$ is equal to
 a) e^{-a} b) e c) e^a d) 1
- If $\lim_{n \rightarrow \infty} \frac{1 - (10)^n}{1 + (10)^{n+1}} = \frac{-a}{10}$, then the value of a is
 a) 0 b) -1 c) 1 d) 2
- The value of $\lim_{n \rightarrow \infty} \frac{\sqrt{n^2 + 1} + \sqrt{n}}{\sqrt[4]{n^3 + n} - \sqrt[4]{n}}$ is
 a) 0 b) 1 c) -1 d) None of these
- The value of $\lim_{x \rightarrow 2} \frac{5}{\sqrt{2} - \sqrt{x}}$ is
 a) $10\sqrt{2}$ b) $+\infty$ c) $-\infty$ d) Does not exist
- $\lim_{n \rightarrow \infty} \frac{2^{-n}(n^2 + 5n + 6)}{(n+4)(n+5)}$ is equal to
 a) 0 b) 1 c) ∞ d) $-\infty$
- If $f(x) = \begin{cases} x \sin \frac{1}{x} & x \neq 0 \\ 0 & x = 0 \end{cases}$, then $\lim_{x \rightarrow 0} f(x)$ is equal to
 a) 1 b) 0 c) -1 d) None of these
- $\lim_{x \rightarrow a} \frac{\log(x-a)}{\log(e^x - e^a)}$ is equal to
 a) 0 b) 1 c) a d) Does not exist

11. The value of $\lim_{x \rightarrow \infty} \left(\frac{x-1}{x+1} \right)^x$, is
a) 0 b) e^{-1} c) e^{-2} d) e^{-3}
12. $\lim_{x \rightarrow 0} \left[\frac{3^x + 3^{-x} - 2}{x^2} \right]$ is equal to
a) $2 \log 3$ b) $-(\log 3)^2$ c) $-2 \log 3$ d) $(\log 3)^2$
13. $\lim_{x \rightarrow 0} \left(\frac{e^x + e^{-x} - 2}{x^2} \right)^{1/x^2}$ is equal to
a) $e^{1/2}$ b) $e^{1/4}$ c) $e^{1/b}$ d) $e^{1/12}$
14. The value of $\lim_{x \rightarrow \infty} \left(\frac{\pi}{2} - \tan^{-1} x \right)^{1/x}$ is
a) 0 b) 1 c) -1 d) e
15. The value of $\lim_{x \rightarrow 1} \left\{ \frac{x^3 + 2x^2 + x + 1}{x^2 + 2x + 3} \right\}^{\frac{1 - \cos(x-1)}{(x-1)^2}}$, is
a) e b) $e^{1/2}$ c) 1 d) None of these
16. $\lim_{x \rightarrow -3} \frac{3x^2 + ax + a - 7}{x^2 + 2x - 3}$ exists, then a is equal to
a) 10 b) 15 c) -15 d) -10
17. $\lim_{x \rightarrow \infty} \left(1 - \frac{4}{x-1} \right)^{3x-1}$ is equal to
a) e^{12} b) e^{-12} c) e^4 d) e^3
18. $\lim_{n \rightarrow \infty} \left\{ \frac{1}{1-n^2} + \frac{2}{1-n^2} + \frac{3}{1-n^2} + \dots + \frac{n}{1-n^2} \right\}$ is equal to
a) 0 b) $-1/2$ c) $1/2$ d) 1
19. $\lim_{x \rightarrow 0} \frac{x \tan 2x - 2x \tan x}{(1 - \cos 2x)^2}$, is
a) 2 b) -2 c) $1/2$ d) $-1/2$
20. $\lim_{n \rightarrow \infty} \frac{3 \cdot 2^{n+1} - 4 \cdot 5^{n+1}}{5 \cdot 2^n + 7 \cdot 5^n}$ is equal to
a) $\frac{3}{5}$ b) $-\frac{4}{7}$ c) $-\frac{20}{7}$ d) 0